We feel very grateful to the reviewer who has given us the valuable suggestions and comments for our paper. We have revised our manuscript accordingly.

Huayong Chen

Responses to the reviewer’ comments:

<table>
<thead>
<tr>
<th>Comments of Anonymous Referee #1:</th>
<th>Author’s Reply</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. p.1, line 2 not sure, if &quot;downriver of a check dam&quot; would better describe the exact location of the scour.</td>
<td>Thanks very much for the reviewer’s comment. The phrase “behind a check dam” has been replaced by “downriver of a check dam” for better description of the exact scour location.</td>
</tr>
<tr>
<td>2. p.1, line 11 in cases where debris flow is used in a word composition (e.g. debris-flow pattern, debris-flow nappe) I learned, that there is a hyphen between debris and flow Please check the manuscript accordingly.</td>
<td>A hyphen was added between debris and flow in a sentence throughout the manuscript where “debris flow” was used as attributive.</td>
</tr>
<tr>
<td>3. p.2, line 29 more common is &quot;initiation zone&quot;, not &quot;formation region&quot;; delete &quot;by debris flow&quot; at the end of the sentence, it’s an unnecessary repetition.</td>
<td>The wrong phrases in the sentence have been revised according to the reviewer’s comments.</td>
</tr>
<tr>
<td>4. p.3, line 56/57 not really clear, what this sentence means. Do you mean that the proposed geometry of such spillways is something that should be used especially for torrents with high sediment disposability?</td>
<td>To avoid misunderstanding, the sentence has been modified in the manuscript.</td>
</tr>
<tr>
<td>5. p.3, line 58 &quot;is&quot; instead of &quot;was&quot;.</td>
<td>The word &quot;was&quot; has been replaced by &quot;is&quot; in this sentence.</td>
</tr>
<tr>
<td>6. p.8, line 165 are the values for the density of the debris-flow densities measured values or assumptions? Both values seems to me more valid for hyperconcentrated flows. I would</td>
<td>The flow densities were measured after debris-flow samples were taken. Frankly, as for debris flows the flow density in our experiments seems lower. The experimental analy-</td>
</tr>
</tbody>
</table>
### Expected Values

Values in the order of 1700 - 1900 kg/m\(^3\).

### Preliminary Achievements

The sis here is considered to be the preliminary achievements. The authors appreciate the reviewer's valuable suggestions to carry out more experiments involving debris-flow densities in the order of 1700 - 1900 kg/m\(^3\) in the future.

### Notes

| #1: | Indicate flow direction and exchange the word "behind" with "downriver of".
|-----|--------------------------------------------------------------------------|
| #2a: | Sabo dam is never used in the text. Use check dam or replace check dam with sabo dam in the text.
| #5: | Describe it as "debris-flow hydrograph". If your LRF gave you min, max and mean values, you could perhaps explain the outliers. And: this hydrograph does not really show a typical steep front of a debris flow. It looks more like a hyperconcentrated flood. Again: add information on the sampling rate of the device.
| #6: | Add an arrow to show flow directions. Very small images. Perhaps increase contrast.
| #7: | Scaling effects are not discussed. Please add a section to explain how the results of the experiments can be used in real dimensions. What is the Froude number of your experiments?
| #12: | I miss a sensitivity study on different debris-flow mixtures (e.g. higher densities, water content variations).
| #13: | I miss information on the LRF. What is the sampling rate (in Hz) of the device? How are the values given in lines 89-90, page 5 and the sampling rate added in lines 135-141, page 7.

The word "behind" has been replaced by "downriver of".

The word "Sabo dam" has been replaced by "check dam".

The caption of Figure 5 was changed to "debris-flow hydrograph". The information on the sampling rate of the device was added in line 90, page 5.

An arrow in each figure was added to show debris-flow directions in Fig.6.

The scaling effects are discussed in the revised vision in lines 207-215, page 11. The Froude number in our experiment ranged from 1.14 to 1.16. It meant that the debris flows in the experiments were supercritical flow (in lines 91-92, page 5).
<table>
<thead>
<tr>
<th>Question</th>
<th>Answer</th>
</tr>
</thead>
<tbody>
<tr>
<td>14. What would happen, if there is driftwood involved? Did you test that or what do you expect in such a case?</td>
<td>Debris flows with driftwood will speed up the blockage and jamming of a check dam. Provided that driftwood is involved in our experiments, the check dam will capture driftwood when it passed through the spillway with debris flows. The subsequent debris flows will overflow from the check dam crest once the spillway is blocked by the driftwood, which will cause scour downriver of a check dam. The debris flows with driftwood was not considered in the current experiments, but definitely the reviewer has raised a very important question. The related experiments will be carried out to investigate the behaviour of debris flows with driftwood and its scour feature in the future.</td>
</tr>
<tr>
<td>15. Can you say something about abrasion rates and the expected life time of such structures?</td>
<td>Abrasion occurs due to the interaction between solid particles in debris flows and the boundary of hydraulic structures. For a spillway with curved bottom, the reaction of centrifugal force exerting on spillway bottom enhance the interaction between the solid particles and the bottom (a component of the reaction force has the same direction as the gravitational force of debris flows near the outlet of the spillway). Although abrasion phenomenon is common, it is difficult to quantify the abrasion rate during an episode of debris flows. Abrasion may be one of the factors lead to the</td>
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</table>
damage of spillway with lateral contraction. However, some methods can be taken to mitigate the abrasion damage of such structures by using anti-abrasion materials, or add the protecting layer. The check dam with lateral contracted spillway, like other check dams, the expected life time mainly depends on the debris-flow scales, flow velocity, particle concentration, etc.
Effects of Y-type spillway lateral contraction ratios on debris flow patterns and scour features downriver of a check dam behind a check dam

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²Institute of Mountain Hazards and Environment, CAS, Chengdu 610041, China

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Abstract. Debris flows often cause devastating damage to property and can injure or kill residents in mountainous areas. The construction of check dams in debris-debris-flow valleys is considered a useful strategy for mitigating the damages downstream. In this paper, a new type of spillway structure with lateral contraction was proposed to distribute debris flows after the check dam storage filled up. Four different lateral contraction ratios of the spillway were considered in experiments that investigated debris-debris-flow patterns, scour characteristics, and energy dissipation rates when debris flows passed through the spillway. The results indicated that lateral contraction considerably influenced the extension of debris-debris-flow nappes. The drop length of the nappe at η=0.7 (η means lateral contraction ratio) was approximately 1.4 times larger than at η=0.4. The collision, friction, and mixing forces between the debris-debris-flow nappes and debris flows in downstream plunge pools dissipated much of the debris-debris-flow kinetic energy, ranging from 42.03% to 78.08% at different contraction ratios. Additionally, based on a dimensionless analysis, an empirical model was proposed to predict the maximum scour depth behind the check dam downriver of a check dam. It indicated that the results calculated by the model exhibited good agreement with the experimental results.

1 Introduction

Debris flows are formed by poorly sorted, water-saturated materials that mobilize in upstream regions of valleys and surge down slopes in response to gravitational attraction (Iverson, 1997). Large scale debris flows were triggered by intensive rainfalls after the “5.12” Wenchuan Earthquake, including the Zhouqu debris flow,
the Wenjia gully debris flow, and the Hongchun gully debris flow (Wang, 2013; Yu et al., 2013; Tang et al., 2015). On August 8, 2010, a large debris flow occurred in the Luojiayu gully, northern Zhouqu County, Gansu Province. The flow destroyed six villages, blocked the Bailongjiang River, resulting in the formation of a lake that inundated over half of Zhouqu County, and displaced or killed 1765 people (Cui et al., 2013). Usually, large-scale debris flow events involve substantial erosion upstream (Ni et al., 2012; Yu et al., 2013), and large volumes of solid materials are transported from the initiation zone/formation region to downstream areas by debris flows.

The construction of check dams is considered one of the most effective ways to store solid materials and control soil erosion in a valley. This structural counter-measure is commonly used to stabilize bank slopes, flatten the gradients of valleys, reduce flow velocity, and decrease the peak-discharge of debris flows (Lenzi, 2002; Mizuyama, 2008; Remaître et al., 2008; Remaître and Malet, 2010). Two main types of check dams are applied to control debris flows (i.e., closed-type and opened-type). Opened-type dams trap boulders, cobble, and gravel, allowing small particles, fine sediments, and water to pass through the dams (Abedini et al., 2012). Closed-type dams not only trap the coarse particles but also retain most small particle materials (Heumader, 2000; Lien, 2003). Generally, the dam storage volume of a closed-type check dam is quickly filled with debris-flow material when a large debris flow occurs. The sequent debris flows directly overflow the check dam, which can lead to serious scour on and around the foundation of the check dam (Figure 1).

Flow patterns and scour caused by the discharge of clear water or sediment flows has been well studied in hydraulic engineering. The characteristics of free-falling nappes behind the spillway of a gravity dam were investigated and the drop length of the free jet was predicted based on the energy equation in which the energy dissipation was neglected at two chosen cross-section (Toombes et al., 2008). Experimental investigations of aeration associated with overflow dams with curved surfaces were carried out, and empirical correlations
predicting the aeration efficiencies of these differently shaped spillways were developed (Chu et al., 2014). An interpolation formula for predicting scour depth was proposed based on experimental data. It indicated that the maximum scour increased with increasing discharge and decreased with increasing downstream tail water depth (Adduce et al., 2005). In addition to the discharge and downstream tail water depth, the characteristic grain size and the plunge angle were also considered for scour depth prediction (Bormann and Julien, 1991). Considerable attention has been given to the flow patterns and scour caused by clear flows or sediment flows behind dams. However, few studies have investigated the debris-flow patterns and scour features behind check dams (Pan et al., 2013), especially for spillway structures with lateral contraction. The flow patterns and scour features caused by debris flows are different from those caused by clear water or sediment flows due to different flow densities, cohesion, and particle volume concentrations. The investigation on characteristics of debris flows discharging and scouring with the new spillway (Y-type spillway) can help us better understand the enrichment of scour control for debris-flow mitigation, interaction between debris flows and the erodible solid materials, which can also help us to find out better methods for debris flow mitigation in some serious geology conditions.

In this paper, a new spillway structure with lateral contraction was proposed. Experiments with different spillway contraction ratios were conducted to study the characteristics of debris-flow nappes and scour after debris flows overflowed the check dam. For each experimental test, video cameras were used to record the trajectories of debris-flow nappes. The energy dissipation rate was analyzed due to the varying lateral contraction ratios. Finally, an empirical model based on dimensionless analysis was proposed to predict the maximum scour depth behind the check dam downriver of a check dam.

2 Experimental setup

The experiments were performed at the Dongchuan Debris Flow Observation and Research Station (DDFORS)
in Dongchuan District, Yunnan Province, China. Generally, the experimental flume consisted of a hopper, a gate, a rectangular channel, and the downstream erodible bed (Figure 2a). The rectangular channel was approximately 4.0 m long, 0.4 m wide, and 0.4 m high, with a slope of 8° (Figure 2b). A check dam made of steel material was located at the end of the rectangular channel. The shape of the spillway inlet was a 0.20 m wide by 0.10 m high rectangle. The outlet was shaped like a capital letter 'Y'. The top width of the outlet was equal to that of the inlet. The bottom width ranged from 0.06 m to 0.12 m due to the different contraction ratios of the spillway. The dimensions of the spillway are shown in Figure 2c.

The lateral contraction ratio \( \eta \) is defined as follows:

\[
\eta = \frac{B - b}{B}
\]

where \( B \) is the width of the spillway inlet and \( b \) is the width of the spillway outlet. When \( b = B \), \( \eta = 0 \).

The storage of the check dam was filled with the solid materials from Jiangjia ravine, with a slope of 3°. The diameter of the solid material was smaller than 20.0 mm. Its particle size distribution is shown in Fig. 3. Particle size distribution may affect the debris flow density and flow motion along the channel. The solid materials used in this experiment was prepared according to the sample of typical debris flows and excluded particles larger than 20.0 mm due to the limitations of the experimental conditions. The diameter of the solid materials in the erodible bed was also smaller than 20.0 mm. In addition, the clay and fine particles (smaller than 1.0 mm) were excluded to avoid the effects of matric suction on the development of the scour hole. The particle size distribution of the erodible bed materials is also shown in Figure 3.

In each experimental test, a laser range finder (LRF) was set at the end of the erodible bed to monitor the depth of the debris flow during the entire process, as shown in Figure 4. The LRF measured the distance between the original bottom and the laser receiver. When debris flows flowed over the channel bottom, the LRF measured the distance between the debris flow surface and the laser receiver. The distance
difference was the flow depth. The measurement range of the LRF was up to 30.0 m, with an accuracy of ±0.001 m. The sampling frequency of the LRF was about 31.0 Hz. The elevation difference between the initial position and the flow surface was the measured flow depth. The Froude number in our experiment ranged from 1.14 to 1.16. It meant that the debris flows in the experiments were supercritical flow. An example of the measured results is shown in Figure 5. It reveals that although the debris flow process is not steady over time, the debris flow over a short period can be considered steady flow. Therefore, the energy conservation equation derived based on the steady flow assumption can be applied to analyze the energy dissipation rate of a debris flow.

3 Experimental results and analysis

4.1 Flow patterns of different contraction ratios

When debris flows overflowed the spillway with a high lateral contraction ratio (η=0.7), the flow depth and velocity increased dramatically. The debris flow nappe clearly extended in the flow direction. Furthermore, the debris flows near both side wall, which were forced to change direction by the walls, collided at the outlet when the debris flows overflowed from the spillway (Figure 6a). Decreasing the lateral contraction ratio caused the flow depth and velocity to decrease at the same flow discharge. Therefore, the drop length of the debris-flow nappe decreased in the flow direction. The drop length at η=0.7 was approximately 1.4 times than at η=0.4 (Table 1). Lateral contraction not only affected the drop length but also broadened the nappe width due to the collision of debris flows at the outlet (Figure 6b-d). When η=0.5, the broadening ratio κ (κ is the ratio of nappe width to the outlet width) reached its maximum value (κ=2.93 in Table 1). The nappe width was equal to that of the spillway (κ=1.0) when there was no lateral contraction at the spillway.

If debris flows flowing out of the spillway are considered free-motion point masses under the influence of gravity, the trajectory of a debris-flow nappe can be expressed as follows (Figure 7):
When $\phi = 0$, equation (2) simplifies to equation (3):

$$x = \frac{\sqrt{2v^2y}}{g}$$

where $v$ is the initial velocity of the debris flow flowing out of the spillway, $\phi$ represents the angle of the initial velocity in the horizontal direction, and $y$ is the water elevation difference.

Equation (3) indicates that the nappe extension in the horizontal direction ‘$x$’ is proportional to the initial velocity $v$ and square root of the water elevation difference $y$. From Fig. 6 and Table 1, we found that when $\eta=0.7$, the nappe extension was longest in the flow direction. From this point of view, a high lateral contraction ratio increased the distance between the plunge point and the dam toe, which effectively protected the dam foundation from scouring. The hydraulic characteristics of the nappe away from the spillway at different lateral contraction ratios were shown in Figure 8 and Figure 9. Figure 8 indicates that increasing the lateral contraction ratio decreased the width of the debris-flow nappe. Furthermore, the higher lateral contraction of the spillway strengthened the collision between flows at the spillway outlet. Air bubbles were entrained in the debris flows when the continuum of the debris flows was broken. Figure 9 shows the extent of the debris-flow nappes. The distribution of the flow velocity in the vertical direction at the outlet increased with increasing flow depth due to the effects of boundary friction. Therefore, the longest flow nappes were formed by the debris flows with relatively large velocities at the flow surface.

4.2 Debris-flow scour features behind the check damdownriver of a check dam

The scour features of debris flows behind the check damdownriver of a check dam represent one of the most...
important indexes, which determines the scour depth at the dam foundation. Figure 10 shows the effects of lateral contraction on the formation of scour holes in an erodible bed. For the same curvature of the spillway surface, decreasing the contraction ratio decreased the maximum scour depth and caused the location of the maximum scour point to shift toward the dam toe due to the decreased debris-flow velocity. The maximum scour depth and its location farther from the dam toe for $\eta=0.7$ were approximately 1.3 and 1.4 times, respectively, larger than for $\eta=0.4$. Although a high lateral contraction ratio extended the debris-flow nappe, it also increased the scour depth in the erodible bed to some extent. In addition, debris-flow density has some effects on the scour depth. Figure 11 indicates the scour depth caused by debris flow with density of 1200 kg/m³ is a bit larger than that caused by debris flow with density of 1500 kg/m³ at a certain lateral contraction ratio (Figure 11). It was explained that the debris flow with lower particle concentration (Lower debris-flow density) initialized and carried more bed materials than that with higher particle concentration (Higher debris-flow density) when the other factors were fixed (Such as longitudinal slope of gully, debris-flow scale, lateral contraction ratio of the spillway).

4.3 Energy dissipation at different contraction ratios

Generally, different energy dissipaters such as the plunge pool (Pagliara et al., 2010; Duarte et al., 2015) or step-pool systems (Yu, 2007; Wang et al., 2009; Wang et al., 2012) are required to dissipate the kinetic energy of the surplus flow and prevent the dam foundation and riverbed from scouring when sudden changes to the channel slope occur. The energy dissipation process of the check dam was estimated using the Bernoulli equation (4). The rationale behind using this equation was previously mentioned.

The Bernoulli equation between two reference cross-sections is written as follows:

$$Z_1 + h_1 + \alpha_1 \frac{v_1^2}{2g} = Z_2 + h_2 + \alpha_2 \frac{v_2^2}{2g} + h_n$$

(5)
If $\Delta Z = Z_i - Z_f$, then equation (4) can be transformed into equation (5):

$$\Delta Z + h_i + \alpha_1 \frac{v_1^2}{2g} = h_2 + \alpha_2 \frac{v_2^2}{2g} + h_w$$

(6)

The energy dissipation coefficient $\zeta$ can be expressed as follows:

$$\zeta = 1 - \frac{h_2 + \frac{v_2^2}{2g}}{\Delta Z + h_i + \frac{v_1^2}{2g}}$$

(7)

where $Z_1$ and $Z_2$ are the elevations of reference cross-sections #1 and #2 (Figure. 2b), respectively; $h_1$ and $h_2$ are the depths of debris flows at reference cross-sections #1 and #2, respectively; $v_1$ and $v_2$ are the velocities of the debris flows at references cross-sections #1 and #2, respectively; $\alpha_1$ and $\alpha_2$ are the kinetic energy correction coefficients ($\alpha_1=\alpha_2 =1$) (Adamkowski et al., 2006); $\Delta Z$ is the elevation difference between the two reference cross-sections; and $h_w$ is the water head loss.

Table 2 indicates that the collision and friction forces between the debris-debris flow nappes and debris flows in the plunge pool dissipated the kinetic energy of the flows, ranging from 42.03% to 78.08% at different contraction ratios. In the case of $V=0.16 \text{ m}^3$, the energy dissipation rate decreased gradually when the contraction ratio changed from 0.7 to 0.4 because the high contraction ratio increased the number of debris-debris-flow collisions when it passed through the spillway. In the cases of $V=0.10 \text{ m}^3$ and $V=0.06 \text{ m}^3$, the energy dissipation rate also decreased with decreasing the contraction ratios except at $\eta=0.4$. The mean value of the energy dissipation rate demonstrated a good positive correlation between the energy dissipation rate and the lateral contraction ratio. In addition, for the same contraction ratio, the energy dissipation rate increased gradually with decreasing debris-debris-flow scale.

4.4 The empirical equation for estimating the maximum scour depth

Many empirical equations have been proposed to predict the maximum scour depth over the last several
decades (Bormann and Julien, 1991; Zhou, 1991; Adduce et al., 2005; Pan et al., 2013). The main parameters include the unit discharge, characteristic particle size of the erodible bed, water elevation difference and clear water and debris-flow densities. However, most of the empirical equations (Li and Liu, 2010) neglect dimensional homogeneity (the empirical equations should be dimensionally homogeneous). For new type of spillway, the lateral contraction ratio is an important parameter for predicting the maximum scour depth. For a debris flow, the maximum scour depth is mainly determined by the following parameters:

\[ h_d = f(q, g, \rho_d, \rho_w, d_{90}, \eta, \ldots) \] (8)

where \( h_d \) is the maximum scour depth, \( q \) is the unit discharge of the debris flow, \( g \) is the acceleration due to gravity, \( \rho_d \) and \( \rho_w \) are the debris-flow density and clear water density, respectively (two debris-flow densities were considered, including \( \rho_d = 1200 \text{kg/m}^3 \) and \( \rho_d = 1500 \text{kg/m}^3 \)), \( d_{90} \) is the characteristic particle size for erodible bed materials, and \( \eta \) is the lateral contraction ratio.

Based on a dimensional analysis, the dimensionless parameters with clear physical meanings are developed as follows:

\[ \frac{h}{d_{90}} = k \left( \frac{q}{d_{90} \sqrt{gd_{90}}} \right)^{a_1} \left( \frac{\rho_d}{\rho_w} \right)^{a_2} (1 - \eta)^{a_3} \] (9)

where \( h/d_{90} \) is dimensionless scour depth, \( k \) is a coefficient, \( a_i \) is an index \( (i=1, 2, 3) \), \( \frac{q}{d_{90} \sqrt{gd_{90}}} \) is the dimensionless discharge, and \( \rho_d/\rho_w \) is the dimensionless density.

According to the experimental data, the regression equation can be expressed as follows:

\[ \frac{h}{d_{90}} = 3.15 \left( \frac{q}{d_{90} \sqrt{gd_{90}}} \right)^{0.51} \left( \frac{\rho_d}{\rho_w} \right)^{1.1583} (1 - \eta)^{0.7883} \] (10)

The regression equation suggests that the flow density had relatively small effects on the depth of the scour hole. However, the debris-flow discharge and the lateral contraction had strong effects on the maximum depth of the scour hole, which directly determined the kinetic energy of the flow in the downstream erodible bed.
The validation tests were also performed using the physical experimental model shown in Figure 2, but under different conditions. Additional experimental data provided in the literature (Ben and Mossa, 2006) were used to verify the reliability of the regression equation. The predicted results exhibited good agreement with the experimental results. The absolute error was smaller than 15.0% in most cases, as shown in Figure 1.

4 Conclusions and Discussions

4.1 Conclusions

The characteristics of debris flows overflowing the new type of spillway were analyzed at different lateral contraction ratios. The energy dissipation rate and an empirical model for predicting the maximum scour depth were also studied in this paper. The following conclusions were drawn from this analysis:

1) Flow patterns were mainly determined by the lateral contraction ratio. At a high lateral contraction ratio, the spillway effectively extended the debris-flow nappe and increased the distance between the plunge point and the dam toe. The drop length of the nappe at $\eta=0.7$ was approximately 1.4 times higher than that at $\eta=0.4$.

2) The plunge pool behind the check dam downriver of a check dam inevitably dissipated the kinetic energy of the debris flow after overflowing the check dam. The collision and friction between the debris-flow nappe and the debris flow in the plunge pool dissipated the kinetic energy of the flow, ranging from 42.03% to 78.08% at different contraction ratios. Generally, increasing the contraction ratio increased the energy dissipation rate at the same debris-flow scale.

3) An empirical model was proposed to predict the maximum scour depth behind the check dam downriver of a check dam. The results indicated that the predicted results exhibited good agreement with the experimental results. The absolute error was smaller than 15.0% in most cases.

4.2 Discussions

The characteristics of debris flow nappe and scour downriver of a check dam with different spillway were
experimentally investigated in this article. When the experimental data are used to predict debris-flow motion
and scour feature downriver of a check dam in prototype, the effects of physical model scale should be
considered. Scaling effect is mainly induced by dissatisfaction of mobility similitude of model sediment in
physical model experiments and it leads to discrepancies between the estimated and actual scour results. Just like
the experimental investigation on the scale effect in pier-scour experiments, the bed-particle mobility similitude
(Ettema et al., 1998; Ettema and Melville, 1999) or the flow-strength similitude (Lee and Sturm, 2009) should be
satisfied to weaken or eliminate the scaling effect for debris-flow scour when the experimental results are
extrapolated to predict prototype performance in the future.

When debris flows occur in the mountainous areas with forest the driftwood carried by debris flows is a
common phenomenon. The debris flows combined with driftwood will speed up blockage and jamming of a
check dam. Once the spillway is blocked by the driftwood the subsequent debris flows will overflow from the
crest of a check dam, which will cause extensive scour downriver of a check dam. Therefore, it is also necessary
to investigate the behavior of debris flows with driftwood and propose some reasonable structural or non-
structural countermeasures to mitigate the effects of debris flows with driftwood on the operation of a check dam
in the future.

Acknowledgments

The study results presented in this paper were supported by the Key Research Program of the Chinese
Academy of Sciences (Grant No. KZZD-EW-05-01), the National Natural Science Foundation of China (Grant
No. 51209195), the Science Technology Service Network Initiative, Chinese Academy of Sciences (Grant No.
KFJ-EW-STS-094), and the Key Laboratory of Mountain Hazards and Earth Surface Process, Chinese Academy
of Sciences.

List of symbols
The index for the dimensionless parameter (-)

The width of the spillway outlet (m)

The width of the spillway inlet (m)

The characteristic particle size for erodible bed materials (m)

The coefficient for the dimensionless equation (-)

The depth of debris flows at reference cross-sections #1 (m)

The depth of debris flows at reference cross-sections #2 (m)

The maximum scour depth (m)

The water head loss (m)

The acceleration of gravity (m/s²)

The unit discharge of the debris flow (m³/s)

The initial velocity of the debris flow flowing out of the spillway (m/s)

The velocity of debris flows at reference cross-sections #1 (m/s)

The velocity of debris flows at reference cross-sections #2 (m/s)

The scale of debris flow in the experiments (m³)

Trajectory in the horizontal direction (m)

The water elevation difference (m)

The elevation of reference cross-sections at #1 (m)

The elevation of reference cross-sections at #2 (m)

The elevation difference between the two reference cross-sections (m)

The kinetic energy correction coefficient for \( v_1 \) (-)

The kinetic energy correction coefficient for \( v_2 \) (-)

The density of debris flows (kg/ m³)

The density of clear water (kg/ m³)

The energy dissipation coefficient(-)

The lateral contraction ratio(-)

The angle of the initial velocity in the horizontal direction(°)
References


Tang, C., Jiang, Z., and Li, W.: Seismic Landslide Evolution and Debris Flow Development: A Case Study in the


Fig. 1. An example of foundation scour **downriver of** behind a check dam.
(a) Photograph of the experimental setup (b) Schematic diagram of the experimental setup (unit: cm)

(c) The structure and dimensions of the spillway (unit: mm). Four different lateral contraction ratios were considered in the experiments: (a) $B=200.0$ mm, $b=60.0$ mm, $\eta=0.7$; (b) $B=200.0$ mm, $b=80.0$ mm, $\eta=0.6$; (c) $B=200.0$ mm, $b=100.0$ mm, $\eta=0.5$; (d) $B=200.0$ mm, $b=120.0$ mm, $\eta=0.4$. The bottom of the spillway was formed by a compound curve surface (a simple curved segment and a circular segment: radius $R=100.0$ mm, radius angle $\delta=75^\circ$).

Fig. 2. Experimental setup
Fig. 3. The particle size distribution of samples for the debris flows and erodible bed.
Fig. 4. Photograph of the LRF system (the photograph was taken in the downstream direction)
Fig. 5. An example of a debris-flow hydrograph—debris flow duration monitored by the LRE.
Fig. 6. Various debris flow patterns at different lateral contraction ratios (the pictures on the left were taken from a downstream view)
Fig. 7. A diagram of dynamic parameters of debris flows
Fig. 8. The transverse expansion of a debris flow nappe at different lateral contraction ratios
Fig. 9. The trajectory of a debris flow nappe
(a) \( \eta = 0.7, V = 0.16 \text{ m}^3, \rho = 1.50 \text{ g/cm}^3, b = 0.06 \text{ m} \)

(b) \( \eta = 0.6, V = 0.16 \text{ m}^3, \rho = 1.50 \text{ g/cm}^3, b = 0.08 \text{ m} \)

(c) \( \eta = 0.5, V = 0.16 \text{ m}^3, \rho = 1.50 \text{ g/cm}^3, b = 0.10 \text{ m} \)

(d) \( \eta = 0.4, V = 0.16 \text{ m}^3, \rho = 1.50 \text{ g/cm}^3, b = 0.12 \text{ m} \)

**Fig. 10.** The shapes of the scour hole behind the check dam downriver of a check dam \( (V=0.16 \text{ m}^3, \rho=1.50 \text{ g/cm}^3) \)
Fig. 11. Comparison of scour depth at different debris-flow densities

- (a) $V=0.1\text{m}^3$
- (b) $V=0.06\text{m}^3$
Fig. 1112. Comparison between predicted data and experimental ones.
Table 1. The main parameters of the debris flow nappe for different contraction ratios

<table>
<thead>
<tr>
<th>Items</th>
<th>(a)</th>
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<tr>
<td>Width of the outlet $b$/mm</td>
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<td>100.0</td>
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<td>Lateral contraction ratio $\eta$</td>
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Notes: $B$ is constant for each spillway type ($B = 200.0$ mm)
Table 2. The energy dissipation rates at different contraction ratios

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<td>52.34%</td>
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<tr>
<td>$V=0.06$ m³</td>
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<td>68.04%</td>
<td>58.84%</td>
<td>60.58%</td>
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</tr>
</tbody>
</table>
Effects of Y-type spillway lateral contraction ratios on debris flow patterns and scour features downriver of a check dam

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Abstract. Debris flows often cause devastating damage to property and can injure or kill residents in mountainous areas. The construction of check dams in debris-flow valleys is considered a useful strategy for mitigating the damages downstream. In this paper, a new type of spillway structure with lateral contraction was proposed to distribute debris flows after the check dam storage filled up. Four different lateral contraction ratios of the spillway were considered in experiments that investigated debris-flow patterns, scour characteristics, and energy dissipation rates when debris flows passed through the spillway. The results indicated that lateral contraction considerably influenced the extension of debris-flow nappes. The drop length of the nappe at $\eta=0.7$ ($\eta$ means lateral contraction ratio) was approximately 1.4 times larger than at $\eta=0.4$. The collision, friction, and mixing forces between the debris-flow nappes and debris flows in downstream plunge pools dissipated much of the debris-flow kinetic energy, ranging from 42.03% to 78.08% at different contraction ratios. Additionally, based on a dimensionless analysis, an empirical model was proposed to predict the maximum scour depth downriver of a check dam. It indicated that the results calculated by the model exhibited good agreement with the experimental results.

1 Introduction

Debris flows are formed by poorly sorted, water-saturated materials that mobilize in upstream regions of valleys and surge down slopes in response to gravitational attraction (Iverson,1997). Large scale debris flows were triggered by intensive rainfalls after the “5.12” Wenchuan Earthquake, including the Zhouqu debris flow,
the Wenjia gully debris flow, and the Hongchun gully debris flow (Wang, 2013; Yu et al., 2013; Tang et al., 2015). On August 8, 2010, a large debris flow occurred in the Luojiayu gully, northern Zhouqu County, Gansu Province. The flow destroyed six villages, blocked the Bailongjiang River, resulting in the formation of a lake that inundated over half of Zhouqu County, and displaced or killed 1765 people (Cui et al., 2013). Usually, large-scale debris flow events involve substantial erosion upstream (Ni et al., 2012; Yu et al., 2013), and large volumes of solid materials are transported from the initiation zone to downstream areas.

The construction of check dams is considered one of the most effective ways to store solid materials and control soil erosion in a valley. This structural counter-measure is commonly used to stabilize bank slopes, flatten the gradients of valleys, reduce flow velocity, and decrease the peak-discharge of debris flows (Lenzi, 2002; Mizuyama, 2008; Remaire et al., 2008; Remaitre and Malet, 2010). Two main types of check dams are applied to control debris flows (i.e., closed-type and opened-type). Opened-type dams trap boulders, cobble, and gravel, allowing small particles, fine sediments, and water to pass through the dams (Abedini et al., 2012). Closed-type dams not only trap the coarse particles but also retain most small particle materials (Heumader, 2000; Lien, 2003). Generally, the dam storage volume of a closed-type check dam is quickly filled with debris-flow material when a large debris flow occurs. The sequent debris flows directly overflow the check dam, which can lead to serious scour on and around the foundation of the check dam (Figure 1).

Flow patterns and scour caused by the discharge of clear water or sediment flows has been well studied in hydraulic engineering. The characteristics of free-falling nappes behind the spillway of a gravity dam were investigated and the drop length of the free jet was predicted based on the energy equation in which the energy dissipation was neglected at two chosen cross-section (Toombes et al., 2008). Experimental investigations of aeration associated with overflow dams with curved surfaces were carried out, and empirical correlations predicting the aeration efficiencies of these differently shaped spillways were developed (Chu et al., 2014). An
interpolation formula for predicting scour depth was proposed based on experimental data. It indicated that the maximum scour increased with increasing discharge and decreased with increasing downstream tail water depth (Adduce et al., 2005). In addition to the discharge and downstream tail water depth, the characteristic grain size and the plunge angle were also considered for scour depth prediction (Bormann and Julien, 1991). Considerable attention has been given to the flow patterns and scour caused by clear flows or sediment flows behind dams. However, few studies have investigated the debris-flow patterns and scour features behind check dams (Pan et al., 2013), especially for spillway structures with lateral contraction. The flow patterns and scour features caused by debris flows are different from those caused by clear water or sediment flows due to different flow densities, cohesion, and particle volume concentrations. The investigation on characteristics of debris flows discharging and scouring with the new spillway (Y-type spillway) can enrich our knowledge of scour control for debris-flow mitigation.

In this paper, a new spillway structure with lateral contraction is proposed. Experiments with different spillway contraction ratios were conducted to study the characteristics of debris-flow nappes and scour after debris flows overflowed the check dam. For each experimental test, video cameras were used to record the trajectories of debris-flow nappes. The energy dissipation rate was analyzed due to the varying lateral contraction ratios. Finally, an empirical model based on dimensionless analysis was proposed to predict the maximum scour depth downriver of a check dam.

2 Experimental setup

The experiments were performed at the Dongchuan Debris Flow Observation and Research Station (DDFORS) in Dongchuan District, Yunnan Province, China. Generally, the experimental flume consisted of a hopper, a gate, a rectangular channel, and the downstream erodible bed (Figure 2a). The rectangular channel was approximately 4.0 m long, 0.4 m wide, and 0.4 m high, with a slope of 8° (Figure 2b). A check dam made of steel material was
located at the end of the rectangular channel. The shape of the spillway inlet was a 0.20 m wide by 0.10 m high rectangle. The outlet was shaped like a capital letter ‘Y’. The top width of the outlet was equal to that of the inlet. The bottom width ranged from 0.06 m to 0.12 m due to the different contraction ratios of the spillway. The dimensions of the spillway are shown in Figure 2c.

The lateral contraction ratio $\eta$ is defined as follows:

$$\eta = \frac{B - b}{B}$$  

(1)

where $B$ is the width of the spillway inlet and $b$ is the width of the spillway outlet. When $b = B$, $\eta = 0$.

The storage of the check dam was filled with the solid materials from Jiangjia ravine, with a slope of 3°. The diameter of the solid material was smaller than 20.0 mm. Its particle size distribution is shown in Fig. 3. Particle size distribution may affect the debris-flow density and flow motion along the channel. The solid materials used in this experiment was prepared according to the sample of typical debris flows and excluded particles larger than 20.0 mm due to the limitations of the experimental conditions. The diameter of the solid materials in the erodible bed was also smaller than 20.0 mm. In addition, the clay and fine particles (smaller than 1.0 mm) were excluded to avoid the effects of matric suction on the development of the scour hole. The particle size distribution of the erodible bed materials is also shown in Figure 3.

In each experimental test, a laser range finder (LRF) was set at the end of the erodible bed to monitor the depth of the debris flow during the entire process, as shown in Figure 4. The LRF measured the distance between the original bottom and the laser receiver. When debris flows flowed over the channel bottom, the LRF measured the distance between the debris-flow surface and the laser receiver. The distance difference was the flow depth. The measurement range of the LRF was up to 30.0 m, with an accuracy of ±0.001 m. The sampling frequency of the LRF was about 31.0 Hz. The elevation difference between the initial position and the flow surface was the measured flow depth. The Froude number in our experiment ranged from 1.14 to 1.16. It
meant that the debris flows in the experiments were supercritical flow. An example of the measured results is shown in Figure 5. It reveals that although the debris-flow process is not steady over time, the debris flow over a short period can be considered steady flow. Therefore, the energy conservation equation derived based on the steady flow assumption can be applied to analyze the energy dissipation rate of a debris flow.

3 Experimental results and analysis

4.1 Flow patterns of different contraction ratios

When debris flows overflowed the spillway with a high lateral contraction ratio ($\eta=0.7$), the flow depth and velocity increased dramatically. The debris-flow nappe clearly extended in the flow direction. Furthermore, the debris flows near both side wall, which were forced to change direction by the walls, collided at the outlet when the debris flows overflowed from the spillway (Figure 6a). Decreasing the lateral contraction ratio caused the flow depth and velocity to decrease at the same flow discharge. Therefore, the drop length of the debris-flow nappe decreased in the flow direction. The drop length at $\eta=0.7$ was approximately 1.4 times than at $\eta=0.4$ (Table 1). Lateral contraction not only affected the drop length but also broadened the nappe width due to the collision of debris flows at the outlet (Figure 6b-d). When $\eta=0.5$, the broadening ratio $\kappa$ ($\kappa$ is the ratio of nappe width to the outlet width) reached its maximum value ($\kappa=2.93$ in Table 1). The nappe width was equal to that of the spillway ($\kappa=1.0$) when there was no lateral contraction at the spillway.

If debris flows flowing out of the spillway are considered free-motion point masses under the influence of gravity, the trajectory of a debris-flow nappe can be expressed as follows (Figure 7):

$$y = xtg\varphi + \frac{g}{2v_1^2\cos\varphi}x^2$$

$$x = \frac{v^2}{g}\cos\varphi\left(\sqrt{\sin^2\varphi + \frac{2gy}{v^2}} - \sin\varphi\right) \varphi \geq 0$$

When $\varphi = 0$, equation (2) simplifies to equation (3):

$$y = xtg\varphi$$
where \( v \) is the initial velocity of the debris flow flowing out of the spillway, \( \varphi \) represents the angle of the initial velocity in the horizontal direction, and \( y \) is the water elevation difference. Equation (3) indicates that the nappe extension in the horizontal direction \( x \) is proportional to the initial velocity \( v \) and square root of the water elevation difference \( y \). From Fig. 6 and Table 1, we found that when \( \eta=0.7 \), the nappe extension was longest in the flow direction. From this point of view, a high lateral contraction ratio increased the distance between the plunge point and the dam toe, which effectively protected the dam foundation from scouring. The hydraulic characteristics of the nappe away from the spillway at different lateral contraction ratios were shown in Figure 8 and Figure 9. Figure 8 indicates that increasing the lateral contraction ratio decreased the width of the debris-flow nappe. Furthermore, the higher lateral contraction of the spillway strengthened the collision between flows at the spillway outlet. Air bubbles were entrained in the debris flows when the continuum of the debris flows was broken. Figure 9 shows the extent of the debris-flow nappes. The distribution of the flow velocity in the vertical direction at the outlet increased with increasing flow depth due to the effects of boundary friction. Therefore, the longest flow nappes were formed by the debris flows with relatively large velocities at the flow surface.

### 4.2 Debris-flow scour features downriver of a check dam

The scour features of debris flows downriver of a check dam represent one of the most important indexes, which determines the scour depth at the dam foundation. Figure 10 shows the effects of lateral contraction on the formation of scour holes in an erodible bed. For the same curvature of the spillway surface, decreasing the contraction ratio decreased the maximum scour depth and caused the location of the maximum scour point to shift toward the dam toe due to the decreased debris-flow velocity. The maximum scour depth and its location
farther from the dam toe for $\eta=0.7$ were approximately 1.3 and 1.4 times, respectively, larger than for $\eta=0.4$. Although a high lateral contraction ratio extended the debris-flow nappe, it also increased the scour depth in the erodible bed to some extent. In addition, debris-flow density has some effects on the scour depth. Figure 11 indicates the scour depth caused by debris flow with density of 1200 kg/m$^3$ is a bit larger than that caused by debris flow with density of 1500 kg/m$^3$ at a certain lateral contraction ratio (Figure 11). It was explained that the debris flow with lower particle concentration (lower debris-flow density) initialized and carried more bed materials than that with higher particle concentration (higher debris-flow density) when the other factors were fixed (such as longitudinal slope of gully, debris-flow scale, lateral contraction ratio of the spillway).

### 4.3 Energy dissipation at different contraction ratios

Generally, different energy dissipaters such as the plunge pool (Pagliara et al., 2010; Duarte et al., 2015) or step-pool systems (Yu, 2007; Wang et al., 2009; Wang et al., 2012) are required to dissipate the kinetic energy of the surplus flow and prevent the dam foundation and riverbed from scouring when sudden changes to the channel slope occur. The energy dissipation process of the check dam was estimated using the Bernoulli equation (4). The rationale behind using this equation was previously mentioned.

The Bernoulli equation between two reference cross-sections is written as follows:

$$Z_1 + h_1 + \alpha_1 \frac{v_1^2}{2g} = Z_2 + h_2 + \alpha_2 \frac{v_2^2}{2g} + h_u$$

(5)

If $\Delta Z = Z_1 - Z_2$, then equation (4) can be transformed into equation (5):

$$\Delta Z + h_1 + \alpha_1 \frac{v_1^2}{2g} = h_2 + \alpha_2 \frac{v_2^2}{2g} + h_u$$

(6)

The energy dissipation coefficient $\zeta$ can be expressed as follows:
where $Z_1$ and $Z_2$ are the elevations of reference cross-sections #1 and #2 (Figure. 2b), respectively; $h_1$ and $h_2$ are the depths of debris flows at reference cross-sections #1 and #2, respectively; $v_1$ and $v_2$ are the velocities of the debris flows at references cross-sections #1 and #2, respectively; $\alpha_1$ and $\alpha_2$ are the kinetic energy correction coefficients ($\alpha_1=\alpha_2=1$) (Adamkowski et al., 2006); $\Delta Z$ is the elevation difference between the two reference cross-sections; and $h_w$ is the water head loss.

Table 2 indicates that the collision and friction forces between the debris-flow nappes and debris flows in the plunge pool dissipated the kinetic energy of the flows, ranging from 42.03% to 78.08% at different contraction ratios. In the case of $V=0.16 \text{ m}^3$, the energy dissipation rate decreased gradually when the contraction ratio changed from 0.7 to 0.4 because the high contraction ratio increased the number of debris-flow collisions when it passed through the spillway. In the cases of $V=0.10 \text{ m}^3$ and $V=0.06 \text{ m}^3$, the energy dissipation rate also decreased with decreasing the contraction ratios except at $\eta=0.4$. The mean value of the energy dissipation rate demonstrated a good positive correlation between the energy dissipation rate and the lateral contraction ratio. In addition, for the same contraction ratio, the energy dissipation rate increased gradually with decreasing debris-flow scale.

### 4.4 The empirical equation for estimating the maximum scour depth

Many empirical equations have been proposed to predict the maximum scour depth over the last several decades (Bormann and Julien, 1991; Zhou, 1991; Adduce et al., 2005; Pan et al., 2013). The main parameters include the unit discharge, characteristic particle size of the erodible bed, water elevation difference and clear water and debris-flow densities. However, most of the empirical equations (Li and Liu, 2010) neglect dimensional homogeneity (the empirical equations should be dimensionally homogeneous). For new type of
spillway, the lateral contraction ratio is an important parameter for predicting the maximum scour depth. For a debris flow, the maximum scour depth is mainly determined by the following parameters:

\[ h_d = f(q, g, \rho_d, \rho_w, d_{90}, \eta, \ldots) \]  

(8)

where \( h_d \) is the maximum scour depth, \( q \) is the unit discharge of the debris flow, \( g \) is the acceleration due to gravity, \( \rho_d \) and \( \rho_w \) are the debris-flow density and clear water density, respectively (two debris-flow densities were considered, including \( \rho_d=1200\text{kg/m}^3 \) and \( \rho_d=1500\text{kg/m}^3 \)), \( d_{90} \) is the characteristic particle size for erodible bed materials, and \( \eta \) is the lateral contraction ratio.

Based on a dimensional analysis, the dimensionless parameters with clear physical meanings are developed as follows:

\[ \frac{h_d}{d_{90}} = k \left( \frac{q}{d_{90} \sqrt{gd_{90}}} \right)^{a_1} \left( \frac{\rho_d}{\rho_w} \right)^{a_2} (1-\eta)^{a_3} \]  

(9)

where \( \frac{h_d}{d_{90}} \) is dimensionless scour depth, \( k \) is a coefficient, \( a_i \) is an index (i=1, 2, 3), \( \frac{q}{d_{90} \sqrt{gd_{90}}} \) is the dimensionless discharge, and \( \frac{\rho_d}{\rho_w} \) is the dimensionless density.

According to the experimental data, the regression equation can be expressed as follows:

\[ \frac{h_d}{d_{90}} = 3.15 \left( \frac{q}{d_{90} \sqrt{gd_{90}}} \right)^{0.51} \left( \frac{\rho_d}{\rho_w} \right)^{0.1363} (1-\eta)^{0.7883} \]  

(10)

The regression equation suggests that the flow density had relatively small effects on the depth of the scour hole. However, the debris-flow discharge and the lateral contraction had strong effects on the maximum depth of the scour hole, which directly determined the kinetic energy of the flow in the downstream erodible bed. The validation tests were also performed using the physical experimental model shown in Figure 2, but under different conditions. Additional experimental data provided in the literature (Ben and Mossa, 2006) were used to verify the reliability of the regression equation. The predicted results exhibited good agreement with the experimental results. The absolute error was smaller than 15.0% in most cases, as shown in Figure 12.
4. Conclusions and Discussions

4.1 Conclusions

The characteristics of debris flows overflowing the new type of spillway were analyzed at different lateral contraction ratios. The energy dissipation rate and an empirical model for predicting the maximum scour depth were also studied in this paper. The following conclusions were drawn from this analysis:

1) Flow patterns were mainly determined by the lateral contraction ratio. At a high lateral contraction ratio, the spillway effectively extended the debris-flow nappe and increased the distance between the plunge point and the dam toe. The drop length of the nappe at $\eta=0.7$ was approximately 1.4 times higher than that at $\eta=0.4$.

2) The plunge pool downriver of a check dam inevitably dissipated the kinetic energy of the debris flow after overflowing the check dam. The collision and friction between the debris-flow nappe and the debris flow in the plunge pool dissipated the kinetic energy of the flow, ranging from 42.03% to 78.08% at different contraction ratios. Generally, increasing the contraction ratio increased the energy dissipation rate at the same debris-flow scale.

3) An empirical model was proposed to predict the maximum scour depth downriver of a check dam. The results indicated that the predicted results exhibited good agreement with the experimental results. The absolute error was smaller than 15.0% in most cases.

4.2 Discussions

The characteristics of debris flow nappe and scour downriver of a check dam with different spillway were experimentally investigated in this article. When the experimental data are used to predict debris-flow motion and scour feature downriver of a check dam in prototype, the effects of physical model scale should be considered. Scaling effect is mainly induced by dissatisfaction of mobility similitude of model sediment in
physical model experiments and it leads to discrepancies between the estimated and actual scour results. Just like
the experimental investigation on the scale effect in pier-scour experiments, the bed-particle mobility similitude
(Ettema et al, 1998; Ettema and Melville, 1999) or the flow-strength similitude (Lee and Sturm, 2009) should be
satisfied to weaken or eliminate the scaling effect for debris-flow scour when the experimental results are
extrapolated to predict prototype performance in the future.

When debris flows occur in the mountainous areas with forest the driftwood carried by debris flows is a
common phenomenon. The debris flows combined with driftwood will speed up blockage and jamming of a
check dam. Once the spillway is blocked by the driftwood the subsequent debris flows will overflow from the
crest of a check dam, which will cause extensive scour downriver of a check dam. Therefore, it is also necessary
to investigate the behavior of debris flows with driftwood and propose some reasonable structural or non-
structural countermeasures to mitigate the effects of debris flows with driftwood on the operation of a check dam
in the future.

Acknowledgments

The study results presented in this paper were supported by the Key Research Program of the Chinese
Academy of Sciences (Grant No. KZZD-EW-05-01), the National Natural Science Foundation of China (Grant
No.51209195), the Science Technology Service Network Initiative, Chinese Academy of Sciences (Grant No.
KFJ-EW-STS-094), and the Key Laboratory of Mountain Hazards and Earth Surface Process, Chinese Academy
of Sciences.

List of symbols

\[ a_i = \text{The index for the dimensionless parameter (--) } \]
\[ b = \text{The width of the spillway outlet (m) } \]
\[ B = \text{The width of the spillway inlet (m) } \]
\[ d_90 = \text{The characteristic particle size for erodible bed materials (m) } \]
\[ k = \text{The coefficient for the dimensionless equation (--) } \]
\[ h_1 = \text{The depth of debris flows at reference cross-sections #1 (m) } \]
\[ h_2 = \text{The depth of debris flows at reference cross-sections #2 (m) } \]
\[ h_d = \text{The maximum scour depth (m) } \]
\( h_w = \) The water head loss (m)
\( g = \) The acceleration of gravity (m/s\(^2\))
\( q = \) The unit discharge of the debris flow (m\(^3\)/s)
\( v = \) The initial velocity of the debris flow flowing out of the spillway (m/s)
\( v_1 = \) The velocity of debris flows at reference cross-sections #1 (m/s)
\( v_2 = \) The velocity of debris flows at reference cross-sections #2 (m/s)
\( V = \) The scale of debris flow in the experiments (m\(^3\))
\( x = \) Trajectory in the horizontal direction (m)
\( y = \) The water elevation difference (m)
\( Z_1 = \) The elevation of reference cross-sections at #1 (m)
\( Z_2 = \) The elevation of reference cross-sections at #2 (m)
\( \Delta z = \) The elevation difference between the two reference cross-sections (m)

Greek letters
\( \alpha_1 = \) The kinetic energy correction coefficient for \( v_1 \) (-)
\( \alpha_2 = \) The kinetic energy correction coefficient for \( v_2 \) (-)
\( \rho_d = \) The density of debris flows (kg/ m\(^3\))
\( \rho_w = \) The density of clear water (kg/ m\(^3\))
\( \zeta = \) The energy dissipation coefficient (-)
\( \eta = \) The lateral contraction ratio (-)
\( \phi = \) The angle of the initial velocity in the horizontal direction (°)
References


Tang, C., Jiang, Z., and Li, W.: Seismic Landslide Evolution and Debris Flow Development: A Case Study in the


Fig. 1. An example of foundation scour downriver of a check dam
(a) Photograph of the experimental setup

(b) Schematic diagram of the experimental setup (unit: cm)

(c) The structure and dimensions of the spillway (unit: mm). Four different lateral contraction ratios were considered in the experiments: (a) $B=200.0$ mm, $b=60.0$ mm, $\eta=0.7$; (b) $B=200.0$ mm, $b=80.0$ mm, $\eta=0.6$; (c) $B=200.0$ mm, $b=100.0$ mm, $\eta=0.5$; (d) $B=200.0$ mm, $b=120.0$ mm, $\eta=0.4$. The bottom of the spillway was formed by a compound curve surface (a simple curved segment and a circular segment: radius $R=100.0$ mm, radius angle $\delta=75^\circ$).

Fig. 2. Experimental setup
Fig. 3. The particle size distribution of samples for the debris flows and erodible bed
Fig. 4. Photograph of the LRF system (the photograph was taken in the downstream direction)
Fig. 5. An example of a debris-flow hydrograph
Fig. 6. Various debris flow patterns at different lateral contraction ratios (the pictures on the left were taken from a downstream view)
Fig. 7. A diagram of dynamic parameters of debris flows.
Fig. 8. The transverse expansion of a debris flow nappe at different lateral contraction ratios
Fig. 9. The trajectory of a debris flow nappe
Fig. 10. The shapes of the scour hole downriver of a check dam ($V=0.16 \text{ m}^3$, $\rho=1.50 \text{ g/cm}^3$)
Fig. 11. Comparison of scour depth at different debris-flow densities

(a) $V=0.1\text{m}^3$  
(b) $V=0.06\text{m}^3$
Fig. 12. Comparison between predicted data and experimental ones
Table 1. The main parameters of the debris flow nappe for different contraction ratios

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<tr>
<td>$V=0.06$ m³</td>
<td>78.08%</td>
</tr>
<tr>
<td>Mean value</td>
<td>73.29%</td>
</tr>
</tbody>
</table>