Size of wildfires in the Euro-Mediterranean region: Observations and theoretical analysis

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Abstract. MODIS satellite observations of fire size and ERA-Interim meteorological reanalysis are used to derive a relationship between burnt area and wind speed over the Mediterranean region and Eastern Europe. Largest wildfire size does not show a strong response with respect to wind speed in Eastern Europe. In the Mediterranean, as intuitively expected, the burnt area associated with the largest wildfires is an increasing function of wind speed for moderate temperature anomalies. In situations of severe heatwaves, the relationship between burnt area and wind speed displays a bimodal shape. Burnt areas are large for low 10-meter wind speed (lower than 2 m s\textsuperscript{-1}), decrease for moderate wind speed values (lower than 5 m s\textsuperscript{-1} and larger than 2 m s\textsuperscript{-1}) and increase again for large wind speed (larger than 5 m s\textsuperscript{-1}). To explain such behavior we use a stochastic model of fire propagation, known as a probabilistic cellular automata. This model uses a probabilistic local rule to derive the total burnt area. The observed relationship between burnt area and wind speed can be interpreted in terms of percolation threshold above which the propagation in the model is infinite, which mainly depends on local terrain slope and vegetation state (type, density, fuel moisture). In eastern Europe, the percolation threshold is never exceeded for observed wind speeds. In the Mediterranean Basin we see two behaviors. During moderately hot weather, the percolation threshold is passed when the wind grows strong. On the other hand, in situations of severe Mediterranean heatwaves, moderate wind speed values impair the propagation of the wildfire against the wind and do not sufficiently accelerate the forward propagation to allow a growth of wildfire size.

1 Introduction

Large wildfires can have a significant impacts on natural, social and economic systems. If most fires are extinguished in the initial stages and remain small, the largest forest fires events represent most of
the area burned and can have catastrophic consequences. The Mediterranean basin is also the major European region where wildfires occur, with about 90% of the European burnt area (Chuvieco 2009). Vegetation fires burnt an average 200,000 ha annually in the Mediterranean Basin between 1960 and 1970; the figure attained over 400,000 ha in the 1970’s and over 600,000 ha in the 1980’s (Le Houérou 1987). Indeed, it increased ten-fold between the 1873-1972 time period and the following three decades (Pausas and Fernandez-Muñoz 2011). Between 1980 and 2003, 57 % of the total burnt area and 38% of all ignited fires in Europe burned in Portugal (EFFIS 2003, San-Miguel-Ayanz et al 2013, Ganteaume et al 2013). The main cause of this trend of Mediterranean wildfires has been attributed to rural depopulation, inducing an increase in fuel amount and causing a change of fire regime from fuel-limited to drought-driven (Pausas and Fernandez-Muñoz 2011). Large wildfire occurrence is also affected by special weather conditions which do not affect most of other fires (Alvarado et al 1998).

Wildfire propagation is impacted by various conditions such as fuel moisture and load, human activities and short to long term weather (Flannigan et al 2009). Wind speed is one of the main factors regarding the weather dependency, as it drives the rate of spread and direction of propagation (Rothermel 1972). Fuel moisture is also an important factor for the propagation of wildfires (Sharples 2008). It depends on short (i.e. hour time scale) to medium (i.e. seasonal time scale) variability of temperature, precipitations and relative humidity.

The relationships between weather, vegetation and wildfire burnt area have been investigated in several works. Flannigan et al (2001) link seasonal burnt area with weather at various time and spatial scales (several years to a few days; global to local) and show that warm, dry and windy days are correlated to higher burnt area, and that certain synoptic conditions such as the breakdown of an upper blocking ridge leads to particularly favorable conditions for wildfires. Flannigan and Harrington (1988) show the weather dependency of monthly burnt area with long sequences of dry and low precipitations days. These relationships have been extrapolated for forecasting future wildfire severity in a changing climate. The review by Flannigan et al (2009) indicates with a high confidence that climate change should lead a positive trend of burnt area. This is already measurable in the western US, as suggested by Westerling et al (2006) and Running (2006). Increase in the fire season duration, higher summer temperature, earlier melting of snowpacks and expansion of the areas susceptible to wildfires to elevated forests combine their effects, leading in this region to higher seasonal burnt area since the mid 1980s.

Fire occurrences in the Mediterranean region are driven by human (e.g. land use) and environmental (e.g. weather and topography) factors (Ganteaume et al 2013). The synoptic weather conditions favorable to Mediterranean wildfires are either blocking (Pereira et al 2005) or trough (Levin and Saaroni 1998). Temperature anomalies (Bedia et al 2014) and summer droughts (Dimitrakopoulos et al 2011) are also critical to explain fire occurrence in the Mediterranean Basin. On longer time scales, the aridity level is also linked with large fire occurrence (Pausas and Paula, 2012). In Greece, Kout-
et al (2013) found a positive correlation between 2 years lagged precipitations and burnt area. This climatic driving of burnt area will be impacted by climate and land cover changes. In particular the combination of several factors including rural depopulation and increased fire frequency due to rising temperatures in southern Europe could lead to a general change in the dominant vegetation species, with a predominance of shrublands over forested areas (Moreira et al 2011). Other studies suggest that the change in fire regime will be different whether the climate shifts towards warmer-drier (less fire activity) or warmer-wetter (more fire activity) conditions in the Mediterranean Basin (Batllori et al 2013), a question which remains unanswered.

In order to further these studies, our aim is to analyze the role of short and mid-term weather on the burnt area in the Euro-Mediterranean region, characterized by a variety of land-uses (natural forests, chaparral, agricultural fields), high exposure to heatwaves (Stéfanon et al 2012) and a high wildfire activity. Wildfires in the Mediterranean region tend to be generally caused by accidents (Silva et al 2010, Ganteaume et al 2013) and in eastern Europe they are mostly linked to agricultural practices (Turquety et al 2014). Here we will not study the causes of wildfire activity but the dependency between fire size and weather, in particular wind speed and temperature anomaly. This study continues the work of Cardil et al (2014) on the link between temperature anomalies and wildfire size and the work of Pausas and Paula (2012) and Loepfe et al (2014) on threshold effects on wildfire propagation (e.g. threshold on aridity level) by analyzing the influence of wind speed on burnt area. To complete our goal, we need a comprehensive database of recent wildfires that occurred in this region and the accompanying weather. The availability of remote sensing observations since the 1990s allows the analysis of large, consistent datasets on wildfire activity. In this study we use the MODIS-retrieved burnt area with the ERA-Interim meteorology to analyze the dependency of fire size with wind speed and temperature anomaly. In order to better understand the variations seen in the observations we need to use a model of fire spread. In this study we choose to focus on probabilistic cellular automata (PCA). Our study relies on the following data-driven observation: under certain circumstances wildfires tend to decrease in size with moderate wind speed. A possible cause of such behavior is sought by simulating with a PCA model the fire propagation with varying wind speeds. The robustness of the study with respect to the model parameters will be tested.

After the introduction in Section 1, Section 2 details the data source, the methodology of data processing and analyzes the wildfire burnt area with respect to wind speed and temperature. Section 3 describes the wildfire model used for the theoretical analysis of the dependence of burnt area with respect to wind speed. Section 4 provides an in-depth discussion of the processes explaining the relationship between the wildfire burnt area and the weather. Section 5 concludes the study.
2 Wildfire burnt area observations: methodology and analysis

2.1 Data source

Meteorological data are the 10-m wind speed and 2-m air temperature from the ERA-Interim re-analysis of the European Center for Mean-Range Weather Forecast (ECMWF), which provides data from 1979 onwards, and continues in real time (Simmons et al 2006, Dee et al 2011). The data are available every 6 hours at a 0.75° × 0.75° longitude/latitude resolution. In the present study, the 1200 UTC data are used only.

Wildfire burnt areas result from the fire detection based on the observations from the MODIS instrument (Moderate Resolution Imaging Spectroradiometer) on board of Aqua and Terra polar heliosynchronous orbiting satellites. Daily burnt areas are identified when land cover, and thus surface reflectance, changes drastically and rapidly due to the wildfires (Roy et al 2008). In the present study, the a modified version of the MCD64 burnt area product is used over a period of 10 years (2003-2012) and provides the daily burnt area on a 500 m horizontal grid (Giglio et al 2010). Only the fraction of each grid cell covered by vegetation is allowed to burn, following Turquety et al 2014. The uncertainty can be high for wildfires smaller than 25 ha, a size that corresponds to one pixel of the MCD64 product. There is no lower bound for the size of the detected wildfires in the dataset, since the fraction of vegetation inside a given pixel can be small. We also use the European Forest Fire Information System (EFFIS) dataset in our study (European Commission 2010, San-Miguel-Ayanz et al 2012). It is provided by the Joint Research Center of the European Commission, and is built using MODIS images at 250 m horizontal resolution. A first step of automated classification is used to isolate fire events and a post-processing using human visualization of the burnt scar is performed. A cross-analysis using the active fire MODIS product, fire event news collected in the EFFIS News module as well as land-cover datasets is finally done to ensure a low number of misclassifications (http://forest.jrc.ec.europa.eu/effis/). The system records burnt areas of approximately 40 ha and larger (Sedano et al 2013). Fires under this threshold exist in this dataset, with a higher associated uncertainty. Data is provided for the 2006-2012 time period on the Mediterranean Basin.

Because the drivers of the wildfires can change over the course of the year, and because the largest wildfires occur in summer, we only consider wildfires detected in July and August.

2.2 Data processing

A regridded version at 10 km resolution of the modified MCD64 product is used. A 3-D (latitude, longitude and time) connected component algorithm is applied to extract distinct fire events (Haralick et al 1992). The principal strength of this method is that it allows the detection of wildfires extending over more than 10,000 ha, since adjacent burning cells are connected. This is of particular importance since only large wildfires are investigated in the present study. Its main weakness is that it does not take into account cloud cover impairment of remote sensing. Another problem is that two
independent fire event occurring close to one another (less than 20 km of distance and less than a
day between the end of the first event and the beginning of the second) are considered the same with
this method. The processing of the EFFIS dataset is simpler. It provides the date coordinates of the
shape of each wildfire. We take as location the centroid of this shape.

To relate the ERA-Interim meteorological data with the fire products, the ERA-Interim data are
extracted at the grid point closest to the wildfire. The ERA-Interim reanalysis is the only homoge-
nized gridded dataset at the Euro-Mediterranean region scale available with wind speed information.
It is relevant to provide the large-scale environment in the vicinity of the wildfire. Wind speed data at
finer resolution would probably add value to refine the relationship between wind speed and wildfire,
especially in terms of wind speed range (which is probably underestimated with the ERA-Interim
dataset).

2.3 Data analysis

Figure 1 shows the cumulated wildfire burnt areas as retrieved by MODIS over the 10-year period
(2003-2012). If a grid point has burnt entirely during this 10-year period, the cumulated burnt area
is 10,000 ha. We see that the most wildfire-prone regions are the Mediterranean Basin and central
eastern Europe. In the following, we differentiate the two regions and the Mediterranean Basin will
be referred as MED, whereas central eastern Europe will be referred as EAST.

In this study large wildfires are considered as extreme fires and are identified when the value of the
burnt area exceeds the upper 95\textsuperscript{th} quantile of the local probability density function. These wildfires
cause the majority of the destruction (more than 50% of the burnt area in the EFFIS and MODIS
datasets). Figure 2 shows the dependence of the 95\textsuperscript{th} quantile of burnt area to the 10-meter wind
speed for an anomaly of the 2-meter air temperature with respect to the climatology (1979–2012)
$\Delta T_2$ smaller than $3^\circ C$ and exceeding $3^\circ C$ (heatwave). In Fig. 2 the wildfire-wind speed pairs are placed in 7 bins according to wind speed, with an equal number of samples in each bin and therefore varying wind speed ranges for each bin. These 7 bins constitute separate sets for which we compute the value of the 95th quantile of fire size and its corresponding 70% confidence interval by bootstrapping this statistic 1000 times. For consistency we also show the median (blue) and 75th (green) quantiles of fire size. It can be noted that they do not show strong responses to the chosen meteorological parameters. We will therefore focus only on largest wildfires only. Large temperature anomalies are generally associated with an anticyclonic anomaly, persisting heat waves (Black et al 2004, Cassou et al 2005, Barriopedro et al 2011, Stéfanon et al 2012) and larger burnt area (Pereira et al 2005). In the EAST domain, extreme wildfire size is nearly independent of the wind speed for $\Delta T_2 < 3 \, K$ and slightly increases with wind speed for $\Delta T_2 > 3 \, K$. In the MED domain, a totally different behavior is found. For $\Delta T_2 < 3 \, K$, extreme wildfire burnt areas increase with wind speed, similarly to what is found in the EAST domain for larger temperature anomalies. For $\Delta T_2 > 3 \, K$, a bimodal dependence is found. A large number of wildfires occur for low wind speed (i.e. weaker than 2 m s$^{-1}$) and for high wind speed (i.e. stronger than 4 m s$^{-1}$). The bimodal dependence of wildfire burnt areas to wind speed in the MED region for situations associated with heatwaves is counter-intuitive since the rate of spread is a growing function of wind speed (Rothermel 1972). To understand these observations, a probabilistic cellular automaton model is adapted in Section 3 to include the impact of wind speed on fire propagation and derive the burnt area.

3 Wildfire burnt area simulations: sensitivity to wind speed

3.1 Probabilistic cellular automaton

Several types of fire models exist. One of them is the probabilistic cellular automaton (PCA), which relies on a stochastic fire propagation set by a probability of propagation which depends on wind speed and direction, terrain slope and vegetation state. Despite its simplicity, such model presents enough similarities with fire propagation dynamics to ensure accurate verification against observations and to allow in-depth analysis of fire propagation dynamics for a moderate computational cost (Berjak and Hearne 2002, Trunfio 2004, Hernández-Encinas 2007a, 2007b, Alexandridis et al 2008).

Unlike coupled fire-atmosphere models such as FIRETEC (Linn et al 2002), the PCA model does not rely on physical processes that govern the fire behavior. However its simple implementation allows easier theoretical analysis.

The PCA implements a grid of cells that can be in a finite number of states and a local rule that determines the probability of transition between states at each time step. In our case we use the most elementary form of PCA for fire simulation, taking into account only the effect of wind speed on fire spread. The grid is a regular square lattice of cells and we choose 3 different states for the cells.

- State 0 corresponds to an unburnt cell;
Figure 2. Wildfire burnt areas (BA) (i.e. 50\textsuperscript{th} (blue), 75\textsuperscript{th} (green) and 95\textsuperscript{th} (red) quantiles of the local probability density function) as a function of 10-m wind speed for the EAST (top row) and MED domains (middle and bottom row) for $\Delta T_2 < 3^\circ$C (left column) and $\Delta T_2 > 3^\circ$C (right column). The pink shaded area shows the 70% confidence intervals for the 95\textsuperscript{th} quantile. For the MED region we display the quantiles derived with the MODIS (middle row) and EFFIS (bottom row) datasets.

- State 1 corresponds to the situation of a burning cell. The cells in this state can propagate the fire;
- State 2 corresponds to the situation of an already burnt cell.

The probability that a cell in state 1 can spread the fire to its neighbors is defined by Eq. (1):

\[ p = \min (\gamma p_0 f (V, \theta), 1) \]  

with $V$ the surface wind speed, $\theta$ the angle between the direction of propagation and the wind and $\gamma$ a corrective factor for diagonal spread. The quantity $p_0$ is a constant and is the spreading probability in absence of wind. The function $f$ of wind is defined in Alexandridis \textit{et al} (2008) as:

\[ f(V, \theta) = \exp[V (c_1 + c_2 \cos \theta - 1)] \]
The quantities $c_1$ and $c_2$ are empirical factors set respectively to 0.045 s m$^{-1}$ and 0.131 s m$^{-1}$ (Alexandridis et al 2008). The shape of $f(V, \theta)$ is shown in Fig. 3 for various values of wind speed. Function $f$ is isotropic with zero wind and gradually expands in the direction of the wind. The corrective factor $\gamma$ is set at $\frac{1}{\sqrt{2}}$ such as the fire propagation is isotropic in absence of wind speed. Without such correcting factor the fire would take a square form in the absence of wind.

Figure 4 shows the fraction of burnt cells $y_2^{final}$ - with $y_i$ the fraction of cells in state $i$ in the PCA grid - as a function of $p_0$ when the fire is extinct in a grid constituted of $101 \times 101$ cells. The quantity $y_2^{final}$ is computed from a Monte Carlo simulation. Figure 4 displays a transition at $p_0 \sim 0.3$ between a mode where very few cells are burnt ($y_2^{final} \sim 0$) and another one where the fire spreads to nearly all the grid ($y_2^{final} \sim 0.9$).

### 3.2 Percolation threshold analysis

Above a certain value of the propagation probability $p$ the fire can thus propagate indefinitely in the PCA. The critical value $p_0^{crit}$ of the $p_0$ constant is shown in Fig. 4 for the zero wind case. This phenomenon is called percolation and can be analyzed theoretically. Pak and Hayakawa (2011) studied the percolation threshold for an elementary form of PCA, with no diagonal propagation or wind speed effect. They state with the help of a mean-field approximation that the fraction of cells in states 1 and 2 are governed by Eqs. (3), (4) and (5).

$$\frac{dy_1}{dt} = 4py_1y_0 - a_{12}y_1$$

(3)
Figure 4. Evolution of the fraction of burnt cells $y_2^{final}$ – with $y_2$ the fraction of cells in state “burnt” in the PCA grid – as a function of $p_0$ when the fire is extinct in a grid constituted of $101 \times 101$ cells. The simulation is performed in the absence of wind. The quantity $p_0$ is the constant part of the local fire propagation probability, which can be seen as a proxy of fuel density, type and moisture. The quantity $p_0^{crit}$ is the percolation (infinite propagation in the PCA) threshold.

$$\frac{dy_2}{dt} = a_{12}y_1$$

$$y_0 + y_1 + y_2 = 1$$

with $y_i$ the fraction of cells in state $i$ in the PCA grid, $p$ the probability of fire spread and $a_{12}$ the probability that a cell in state 1 at time $t$ goes to state 2 at time $t+1$. In our case, the quantity $a_{12}$ is set to 1. In the study, we adapt the PCA model to account for wind speed effect and diagonal propagation. Equation (3) is thus modified as follows:

$$\frac{dy_1}{dt} = C(V)p_0y_1y_0 - y_1$$

with $C(V)$ a weighting coefficient which allows to account for fire spreading in various directions as a function of the wind speed. It writes:

$$C(V) = \exp(Vc_1) + 2\exp[V(c_1 - c_2)] + \exp[V(c_1 - 2c_2)] + 2\gamma\exp\left\{V\left[c_1 + c_2\left(\frac{\sqrt{2}}{2} - 1\right)\right]\right\} + 2\gamma\exp\left\{V\left[c_1 - c_2\left(\frac{\sqrt{2}}{2} + 1\right)\right]\right\}$$

The first term of the sum on the right-hand-side of Eq. (7) corresponds to a propagation along the wind direction, the second term to a propagation across the wind direction and the third to a propagation against the wind. The other terms correspond to diagonal propagation ($\sqrt{2}/2$ corresponds to
cos(\pi/4)). The details of the derivation of Eq. (7) is provided in the Appendix. Equation (7) can be simplified:

\[
C(V) = \exp(Vc_1) \times \left\{ \left[ 1 + \exp(-Vc_2) \right]^2 + \sqrt{2} \left[ \exp\left( Vc_2 \left( \frac{\sqrt{2}}{2} - 1 \right) \right) + \exp\left( -Vc_2 \left( \frac{\sqrt{2}}{2} + 1 \right) \right) \right] \right\}
\]  

(8)

Following the methodology of Pak and Hayakawa (2011), we derive a relationship between \(p_0^{crit}\) and the wind speed-dependent coefficient \(C(V)\):

\[
p_0^{crit} = \frac{1.51552}{C(V)}
\]  

(9)

The value of the numerator comes from site percolation theory. For further insight, Pak and Hayakawa (2011) give an introduction to bond and site percolation theory. This equation is plotted in Fig. 5 along with the numerically derived \(p_0^{crit}\). To compute this quantity numerically we consider that percolation occurs when a fire initiated in the middle of our 101 \(\times\) 101 PCA grid, reaches the edges of the domain. The \(p_0\) value increases from 0.2 with 0.001 increments. The critical value \(p_0 = p_0^{crit}\) is set when more than 90% of a 300 simulation ensemble percolate. We can see that both the theoretical and computed values \(p_0^{crit}\) increase with wind speed for low wind values, reach a maximum and then decrease with wind speed. The difference between the theoretical and computed curves is the methodology of derivation of \(p_0^{crit}\). The shape of this curve will be essential in the analysis of our observations in Section 2. In the following, we refer to \(p_{0,0}\) as the value in the absence of wind and

![Figure 5](image-url)

**Figure 5.** \(p_0^{crit}\), the percolation (infinite propagation in the PCA) threshold as a function of wind. Dashed curve is the theoretical value found using mean-field approximation and the full curve is the numerically derived value. Dotted lines \((p_{0,1}, p_{0,2})\) and \((p_{0,3})\) correspond to the curves plotted in Fig. 6. \(p_0^{crit}\) as the maximum value reached by \(p_0^{crit}\).
4 Discussion

The PCA gives us a theoretical framework to understand the results of Fig. 2. The mean fire size of the biggest wildfires (above the 95th quantile) is a growing function of wind speed in most cases, excepted in the Mediterranean Basin for large temperature anomalies. It is also dependent of the slope of the local topography but this has no consequence on the observed behavior of the burnt area. A proposed expression of $p_0$ is described in Alexandridis et al (2008):

$$p_0 = p_h(1 + p_{den})(1 + p_{veg})p_s(\theta_s)$$  \hspace{1cm} (10)

where $p_h$ is a constant used for homogeneous fuel beds, $p_{den}$ and $p_{veg}$ are factors depending on vegetation density and type, respectively. The quantity $\theta_s$ is the local slope in degrees and the expression of $p_s(\theta_s)$ is given by:

$$p_s(\theta_s) = \exp(a\theta_s)$$  \hspace{1cm} (11)

This formulation is very simple and other factors such as fuel moisture could be taken into account for more realistic simulations. We do not consider the effect of slope in this study. It may be a differentiating factor between EAST and MED, which could lead to quantitative differences between fire sizes in the two regions but for a given region the slope value is the same whatever the wind speed, vegetation state or temperature and soil moisture anomaly. The main cause for such behavioral differences is the value of $p_0$ relative to $p_{crit}^0$. The final burnt area can vary drastically because of percolation as seen in Fig. 4. Figure 6 displays the fraction of burnt cells (normalized to its value after 50 time steps in the absence of wind speed and for $p = 1$, see Fig. 5 as a function of wind speed for 3 different values of $p_0$. Three $p_0$ values are chosen in the 3 different domains : $p_{0,1}$ set at 0.26, below the 0 wind percolation threshold, $p_{0,2} = 0.3$ between $p_{0,0}^{crit}$ and $p_{0,max}^{crit}$ and $p_{0,3} = 0.35$ above the maximum of the percolation threshold. (Fig. 5 & Fig. 6). The saturation for strong winds visible is due to the fact that $p = 1$ in the direction of the wind so has always the same shape after 50 time steps and the fraction of burnt cells saturates. For $p_0$ values smaller than $p_{0,0}^{crit}$, percolation is only possible for high winds so the burnt area increases with wind speed similarly to what is observed over the EAST domain and over the MED domain for low temperature anomaly ($\Delta T_2 < 3^\circ$C). For intermediate $p_0$ values ranging between $p_{0,0}^{crit}$ and $p_{0,max}^{crit}$, large burnt area are simulated for low wind values (smaller than about 5 m s$^{-1}$) and large wind speed values (larger than about 15 m s$^{-1}$) (Fig. 6). Conversely, smaller burnt area are simulated for intermediate wind ranging between 5 and 15 m s$^{-1}$ (Fig. 6). For $p_0$ values larger than $p_{0,max}^{crit}$, similar qualitative results are obtained with however larger burnt area.

We can therefore analyze Fig. 2 as if each subfigure corresponds to a different value of $p_0$. The value of $p_0$ corresponding to the EAST domain and MED domain for low temperature anomaly should be lower than $p_{0,0}^{crit}$, so that the burnt area increases with wind speed. The rate of burnt area increase with respect to wind speed is a function of the departure of $p_0$ from $p_{0,0}^{crit}$. Over the EAST
domain, the value of $p_0$ is expected to be farther below $p_{0,0}$ than over the MED domain. It may also explain why a change of propagation regime is observed over the MED domain when shifting from low to high temperature anomalies. Indeed, for large temperature anomalies corresponding to severe heatwaves ($\Delta T_2 > 3^\circ$C) over the MED domain, a value of $p_0$ exceeding $p_{0,0}$ is expected. A simple way to understand such behavior is to consider the probability of extinction of a fire occupying one cell. Let $p$ be the spread probability. The cell has 8 neighbors on a square grid. In the absence of wind, the extinction probability is $(1 - p)^8$. When wind blows, the fire spreads in the direction of the wind and diagonally. The probability of extinction becomes $(1 - p)^3$. Let us consider very weak wind speed values for which isotropic spreading can be assumed and $p$ increases with wind speed. Then the extinction probability $(1 - p)^8$ drops very quickly. When isotropic spreading does not stand anymore, then the probability of extinction transitions to $(1 - p)^3$ and increases as 3 is a lower exponent than for the isotropic spreading. With increasing wind speed, the probability of extinction decreases again. So instead of enhancing wildfire propagation, moderate winds produce smaller wildfires by cutting off the propagation against the wind. Such analysis explains the 2 modes observed in the MODIS and EFFIS data over the MED domain.

The function of wind $f(V, \theta)$ in the calculation of $p$ is critical in the explanation of the observed behavior [see Eq. (9)]. The choice of this function by Alexandridis et al (2008) was done empirically to match with the behavior of the rate of spread of real wildfires as a function of the wind and the angle between the wind direction and the direction of propagation. Its shape is coherent with real wildfire propagation but concerns can be raised (Fig. 3). The backpropagation is very small and the overall shape is non-elliptical. This last point could be due to the indirect impact of factors that

![Figure 6](image_url)

**Figure 6.** Fraction of burnt cells $y_2/y_{20}$ (normalized to its value after 50 time steps in the absence of wind speed and for $p = 1$) as a function of wind speed for $p_0$ values set at $p_{0,1} = 0.26$ (solid line), $p_{0,2} = 0.3$ (dashed line) and $p_{0,3} = 0.35$ (dotted line) in Fig. 5.
Figure 7. Ratio \( \left( p_{0,\text{max}}^{\text{crit}} - p_{0,0}^{\text{crit}} \right) / p_{0,0}^{\text{crit}} \) for different values of the \( c_1 \) and \( c_2 \) parameters governing the function of local fire propagation probability. \( p_{0,\text{max}}^{\text{crit}} \) is the maximum of the percolation threshold for increasing wind speeds and \( p_{0,0}^{\text{crit}} \) is its value for 0 wind. The black diamond shows the \((c_1, c_2)\) pair chosen by Alexandridis et al (2008). A strictly positive value indicates that \( p_{0,0}^{\text{crit}} \) has a maximum value for a non-zero wind speed, which ensures that the burnt area has a local minimum for moderate values of wind speed.

Another concern is that the propagation speed in the direction of the wind tends to grow very quickly with the wind speed. With the expression of \( f(V, \theta) \) used in this study, the propagation speed only becomes very high when the wind speed exceeds 15 m s\(^{-1}\) which is much too high compared to observed wildfires. Tests have been performed by using other expressions of \( f(V, \theta) \), such as the elliptical form and varying the \( c_1 \) and \( c_2 \) coefficients of Eq. (2), and no qualitative difference in the behavior of \( p_{0,0}^{\text{crit}} \) has been evidenced (not shown). In detail, the choice of \( c_1 \) and \( c_2 \) coefficients can be questioned, as it was only validated on one case study. A key issue is to know if \( p_{0,\text{max}}^{\text{crit}} \) is reached for a positive value of the wind speed, which conditions the existence of the "2 modes" regime.

Figure 7 shows the value of the ratio \( \left( p_{0,\text{max}}^{\text{crit}} - p_{0,0}^{\text{crit}} \right) / p_{0,0}^{\text{crit}} \) as a function of \( c_1 \) and \( c_2 \) calculated from Eq. (9). For a value of \( c_2 \) larger than about 1.25\( c_1 \) this property is verified. This condition can be interpreted as the backpropagation of the wildfire being impaired in a sufficiently large angle domain by the wind.

A possible reason for the burnt area to decrease with wind speed for moderate wind speed over the MED domain is that in order to reach a \( p_0 \) value larger than \( p_{0,0}^{\text{crit}} \), higher flammability of the fuel bed or a more fire-prone environment are needed. This could be caused by the lower precipitation...
amounts in the MED region, which would lead to lower fuel moisture. This could also be due to different vegetation type between the EAST and MED regions.

Our analysis reveals the critical role of the percolation threshold in wildfire propagation. Here we focused our work on the dependency between burnt area and wind speed but other studies found threshold behaviors related to other explanatory variables such as the Drought Code of the Canadian Fire Weather Index (Loepfe et al 2014) and fire season aridity (Pausas and Paula 2012). These variables relating to fuel moisture, it could be possible a similar percolation threshold behavior with a PCA incorporating a propagation probability decreasing with fuel moisture.

5 Conclusions

The behavior of the burnt area with temperature anomaly and wind speed was analyzed with the help of MODIS observations and ERA-Interim reanalysis. In the EAST region and in MED for low temperature anomalies, the burnt area is a growing function of wind, which is rather intuitive. For large temperature anomalies in the MED region, corresponding to severe heatwaves, the burnt area behaves differently. It displays a "2 modes" shape with a minimum value of burnt area for medium values of the wind speed. The possible cause of such counter-intuitive behavior has been investigated theoretically by means of probabilistic cellular automata (PCA). It was found that when the wind speed is moderate, the backpropagation is impaired when the forward propagation is not sufficiently fast to compensate the loss in burnt area. Therefore if the wind is not strong enough to make the propagation along the wind direction "sure enough", percolation does not happens in the PCA resulting in smaller wildfires. The percolation threshold is never reached in the EAST region. It is only exceeded for very low or high wind speeds in the MED region. Such shift between 2 regimes of propagation may be caused by the favorable occurrence of severe heatwaves in the MED region.

A natural follow-up of this study would be to model the impact of fuel moisture on the propagation probability by adapting the known variations of the rate of spread of the fire with this quantity (Sharples 2008). It could be complemented by a thorough analysis of the behavior of dead and live fuel moisture in Mediterranean ecosystems with respect to air temperature anomaly and the incorporation of such relation in the expression of the probability of fire propagation. However, fuel moisture is a quantity which is hard to assess. Live fuel moisture depends on the plant species and dead fuel moisture on the size of the fuel particle. For a more holistic approach, a more realistic fire propagation modelling framework such as FIRETEC would be needed to better identify and quantify the processes driving fire propagation. Finally, conducting observational studies on other hotspots of wildfire activity (e.g. Australia, USA) in order to see whether the 2 modes exists in other parts of the world would be of interest.
Appendix A

In this Appendix, the calculation of $C(V)$ is detailed. The quantity $C(V)$ corresponds to the sum of the probabilities that the fire propagates from a neighboring cell to the center cell (Fig. 8).

![Diagram of fire propagation](image)

**Figure 8.** Schematic of the calculation of $C(V)$.

For all 8 neighbors we can write:

$$p_i = k_ip_0$$  \hspace{1cm} (A1)

with $k_i$ being a coefficient depending on the direction of propagation. One can write

$$k_i = \gamma_i \exp \left\{ V \left[ \frac{c_1 + c_2 (\cos \theta_i - 1)}{2} \right] \right\}$$  \hspace{1cm} (A2)

with $\theta_i$ being the angle between the direction of propagation and the direction of the wind for the $i$ component and $\gamma_i$ being equal to $\gamma$ or 1 depending on whether the propagation direction is diagonal or not in the PCA grid. One can write:

$$k_1 = k_7 = \gamma \exp \left\{ V \left[ c_1 - c_2 \left( 1 - \sqrt{2}/2 \right) \right] \right\}$$  \hspace{1cm} (A3)

$$k_2 = k_6 = \exp [V (c_1 - c_2)]$$  \hspace{1cm} (A4)

$$k_3 = k_5 = \gamma \exp \left\{ V \left[ c_1 - c_2 \left( 1 + \sqrt{2}/2 \right) \right] \right\}$$  \hspace{1cm} (A5)

$$k_4 = \exp [V (c_1 - 2c_2)]$$  \hspace{1cm} (A6)
\[ k_8 = \exp(Vc_1) \]  

(A7)

The quantity \( C(V) \) is the sum of the \( k_i \) coefficients and thus writes:

\[
C(V) = \exp(Vc_1) + 2 \exp[V(c_1 - c_2)] + \exp[V(c_1 - 2c_2)] \\
+ 2\gamma \exp \left\{ V \left[ c_1 + c_2 \left( \frac{\sqrt{2}}{2} - 1 \right) \right] \right\} \\
+ 2\gamma \exp \left\{ V \left[ c_1 - c_2 \left( \frac{\sqrt{2}}{2} + 1 \right) \right] \right\} 
\]

(A8)

which can be simplified into:

\[
C(V) = \exp(Vc_1) \times \left\{ \left[1 + \exp(-Vc_2)\right]^2 + \sqrt{2} \left( \exp[Vc_2 \left( \frac{\sqrt{2}}{2} - 1 \right)] + \exp[-Vc_2 \left( \frac{\sqrt{2}}{2} + 1 \right)] \right) \right\} 
\]

(A9)

using \( \gamma = 1/\sqrt{2} \).

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