Developing system robustness analysis for drought risk management: an application on a water supply reservoir

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Received: 21 October 2014 – Accepted: 4 December 2014 – Published: 7 January 2015

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Published by Copernicus Publications on behalf of the European Geosciences Union.
Abstract

Droughts will likely become more frequent, of greater magnitude and of longer duration in the future due to climate change. Already in the present climate, a variety of drought events may occur with different exceedance frequencies. These frequencies are becoming more uncertain due to climate change. Many methods in support of drought risk management focus on providing insight into changing drought frequencies, and use water supply reliability as key decision criterion. In contrast, robustness analysis focuses on providing insight into the full range of drought events and their impact on a system’s functioning. This method has been developed for flood risk systems, but applications on drought risk systems are lacking. This paper aims to develop robustness analysis for drought risk systems, and illustrates the approach through a case study with a water supply reservoir and its users. We explore drought characterization and the assessment of a system’s ability to deal with drought events, by quantifying the severity and socio-economic impact of a variety of drought events, both frequent and rare ones. Furthermore, we show the effect of three common drought management strategies (increasing supply, reducing demand and implementing hedging rules) on the robustness of the coupled water supply and socio-economic system. The case is inspired by Oologah Lake, a multipurpose reservoir in Oklahoma, United States. Results demonstrate that although demand reduction and supply increase may have a comparable effect on the supply reliability, demand reduction may be preferred from a robustness perspective. To prepare drought management plans for dealing with current and future droughts, it is thus recommended to test how alternative drought strategies contribute to a system’s robustness rather than relying solely on water reliability as the decision criterion.
1 Introduction

1.1 Drought management under uncertainty

Droughts affect more people than any other kind of natural disaster owing to their large scale and long-lasting nature (WMO, 2013). In 2012, drought losses in the US were estimated at USD 30 billion (NOAA, 2013), making it the most extensive drought year since 1930. There is a possibility that droughts will intensify in the 21st century due to reduced precipitation and/or increased evapotranspiration (IPCC, 2012). This means that droughts may become more frequent, of greater magnitude and/or of longer duration. Future uncertainty, combined with natural climate variability, is a challenge for long-term decision making on drought management.

In view of climate change, it is increasingly acknowledged that each country should develop and implement national drought management plans to reduce drought risk to an acceptable level (Wilhite et al., 2014; Sivakumar et al., 2014; OECD, 2013). Such drought plan development can be supported by “stress-testing” water supply systems on drought events that are more severe and/or longer in duration than historic droughts (e.g., Watts et al., 2012; Steinschneider and Brown, 2013). However, decision making criteria are lacking to compare and rank various drought management measures.

Decision making on drought management often relies on a measure of water supply reliability (Iglesias et al., 2009; Rossi and Cancelliere, 2012): the probability of meeting the water demand. Reliability can be increased by either reducing the demand (e.g. by water conservation, reuse of wastewater and reduction of distribution losses) or increasing the supply (e.g. by building new reservoirs, expanding existing reservoirs, constructing desalination plants). However, this reliability metric is based on estimates of long-term demand and supply patterns, and does not give insight into the (socio-economic) impact of water shortage once it occurs. Besides managing towards an acceptable balance between demand and supply, it is important to understand the impact of temporary situations of water shortage and the effect of short-term measures that aim to reduce these impacts, such as delivery restrictions/rationing, temporary...
additional sources of supply, and prioritization among users. In addition to long-term supply reliability, decision making criteria are thus needed to provide insight into the effect of drought management measures during droughts. This paper proposes new criteria to support decision-making on drought risk management.

1.2 Analysing system robustness

A method to obtain insight into the impact of a range of hydro-meteorological events on a system’s functioning has been proposed in Mens et al. (2011): system robustness analysis. The concept of robustness originates from the engineering literature, where it is defined as the ability of systems to maintain desired system characteristics when subjected to disturbances (Carlson and Doyle, 2002). A similar concept, resilience, originates from the socio-ecological resilience community and is defined as the ability of ecosystems or socio-ecological systems to absorb disturbances without shifting into a different regime (Holling, 1973; Walker and Salt, 2006; Folke, 2006; Scheffer et al., 2001). Robustness and socio-ecological resilience are comparable concepts (Anderies et al., 2004), but robustness is considered more suitable for systems in which some components are designed (Carpenter et al., 2001). Since we focus on water management systems (including drought risk systems), which usually contain many engineering components, we prefer the term robustness. Furthermore, resilience in water management has been defined as the ability to recover from the impact of flood events (De Bruijn, 2004), which stays closest to its original (latin) meaning: “to jump back”.

In a flood risk context, systems are disturbed by river flood waves, and they may shift into a different regime when the impact from flooding is too large to recover from (Mens et al., 2011). Resilience, in the narrow definition, can be considered one of the system characteristics that add to a system’s robustness; the ability of a system to remain functioning depends on its ability to recover from the response to a disturbance. Another characteristic that adds to system robustness is *resistance*, the ability to withstand disturbances without responding at all (zero impact) (see De Bruijn, 2005).
The robustness analysis method aims to provide insight into the sensitivity of a system to extreme events that result from climate variability, for example floods and droughts. Because climate change may affect the frequency of these events, robustness analysis focuses on a range of events that are plausible both now and in the future. Understanding the relationship between extreme events and their impact on the system is believed to aid in drafting robust strategies that increase the system’s ability to deal with both frequent and rare events, now as well as in the future.

The first step in a robustness analysis is to draw a relationship between drought severity and corresponding impact: the response curve (Fig. 1). This curve visualizes the impacts that can be expected under a range of drought events. Next, the curve is described by the following robustness criteria:

1. Resistance threshold: under which drought conditions will socio-economic impacts first start to occur? In other words: to what extent can the system withstand droughts?

2. Proportionality: how gradual does the impact increase with increasing drought severity?

3. Manageability: under which range of drought conditions are impacts still manageable? In other words: when do impacts exceed a societally unacceptable level?

In a flood risk system, the resistance threshold relates to the protection standard. A proportional response curve of a flood risk system implies that sudden impacts are avoided, because a slight change in river discharge does not result in substantially different flood impact. Finally, flood impacts are manageable when they are below a critical level for a large range of flood magnitudes. The robustness analysis method has been successfully applied on two systems exposed to river flooding, where it was demonstrated that the robustness criteria have additional value compared to the more traditional decision making criteria based on single-value risk (Mens and Klijn, 2014; Mens et al., 2014).
Since system robustness analysis has been developed in a flood risk management context, it is unclear whether and how it can be applied on drought risk systems. The aim of this paper is therefore to develop the robustness analysis method for drought risk systems. We illustrate the approach with a case inspired by Oologah Lake in Oklahoma (United States) and its water users.

### 1.3 Application on a drought risk system

To explore the potential of robustness analysis in a drought management context, this paper develops the approach for a system exposed to droughts. The system includes a water supply reservoir and water users. As an illustration of the approach, we apply it on a case inspired by the Oologah reservoir in Oklahoma, United States. The data available from this reservoir was adapted to be able to show the effect of different drought management strategies (smaller demand, higher capacity, hedging rules) on the robustness.

Oologah Lake is a reservoir northeast of the city of Tulsa, Oklahoma, in the United States. This reservoir was constructed between 1950 and 1972 as one of many reservoirs aiming at flood control of the Verdigris River. The Verdigris River is a tributary of the Arkansas River, which flows into the Mississippi River. Besides flood control, the reservoir has three other functions: water supply, navigation and recreation. The reservoir is operated such that the water level is low enough to buffer high runoff events (flood control) and high enough to provide a buffer for droughts (water conservation). We focus on water supply for municipal use. According to historic streamflow measurements, the average annual inflow sum is about $2.8 \times 10^9$ m$^3$. The reservoir capacity is about $6.7 \times 10^8$ m$^3$. For the purpose of the illustrative case, we reduced the reservoir capacity to $5.4 \times 10^8$ m$^3$ (see Sect. 2.2). In this way, a wider range of extreme drought events is available that cause different levels of shortage in water supply.

Drought management strategies lead to new system configurations with different characteristics. We consider the following strategies:
− S1 Demand reduction: water demand is reduced on a structural basis, for example by more efficient distributing systems, motivating inhabitants to reduce domestic water use, and by rainwater harvesting (so tap water is not used for watering gardens and lawns).

− S2 Hedging: outflow is temporarily reduced when a critical reservoir level is reached; thereby accepting smaller losses now to avoid major losses later on.

− S3 Reservoir expansion: the conservation storage is increased at the cost of the flood control buffer, making more water available. Demand remains the same as in the reference. No hedging rules apply.

2 Methods and assumptions

2.1 Water balance model and input data

A simple water balance model calculates storage over time as a function of inflow and outflow. The storage is the volume of water in the reservoir that is available for water supply, the inflow is the volume of water per time step flowing into the reservoir, and the outflow is the users’ intake from the reservoir (also a volume of water per time step). In the reference situation no hedging rules are assumed: this means that demand is met until the reservoir is empty. Each simulation assumes a full reservoir at the start. If the conservation storage is exceeded, the model releases water accordingly.

Overview of parameters in the reference configuration:

− Reservoir capacity = $5.4 \times 10^8$ m$^3$

− Required outflow (demand) = $17.4$ m$^3$ s$^{-1}$

Parameters for the configurations with alternative drought management strategies:

− S1 Demand reduction from $17.4$ to $15$ m$^3$ s$^{-1}$
– S2 Hedging: at 25 % storage the outflow is reduced by 60 %
– S3 Reservoir expansion by 20 % (from $5.4 \times 10^8$ m$^3$ to $6.7 \times 10^8$ m$^3$)

Values for S1 and S3 are chosen such that their resulting water supply reliability (% time outflow > demand) is similar. Implementing hedging rules will reduce the supply reliability, but will potentially mitigate the severity of impacts over the duration of the event.

The input of the water balance model is a time series of monthly averaged streamflow. We used 60 year historic river flow measurements upstream Oologah Lake, as available from waterdata.usgs.gov (gauge Lenapah, Oklahoma, USGS 07171000). From a previous Oologah Lake study (Qiao et al., 2014), projected future series were available: 112 realisations of 150 year time series of reservoir inflow. These series originate from a range of climate models from which the output was used in a hydrological model of the Verdigris catchment. The hydrologic response of Oologah Lake watershed to climate change was analysed by using downscaled climate projections in the Variable Infiltration Capacity (VIC) land surface model. We used the 112 monthly hydrographs from projections of the World Climate Research Program Coupled Model Intercomparison Phase 3 (WCRP-CMIP3), including IPCC’s CO$_2$ emission scenarios A1b, A2 and B1. We obtained this set from USBR (2012). The same dataset was used by Williams (2013) for his study on the effect of climate change on water availability from Oologah Lake.

This paper does not aim to analyse the effect of climate change on drought and drought impact. Instead, we use the historic and future inflow series to obtain a range of plausible drought events for which the impact can be simulated with the water balance model and the loss functions (described below). This will help to obtain insight into how impacts vary with different drought magnitudes, which can be used to conduct climate risk assessments.
2.2 Characterising and selecting drought events

To select drought events from a long time series, different methods have been developed. Hisdal and Tallaksen (2000) give an overview of the most common methods, for example the threshold level method (TLM) and the Sequent Peak Algorithm (SPA). The threshold level method assumes a user-defined threshold (for example the long-term mean); a drought event occurs when the streamflow is below this threshold (Yevjevich, 1967; Dracup et al., 1980). The downside of TLM is that for longer droughts the flow may temporarily exceed the threshold, which divides the longer droughts into smaller mutually dependent droughts (Hisdal and Tallaksen, 2000). To avoid this problem, smaller drought events can be pooled. SPA can be considered a pooling method.

SPA (Loucks and Van Beek, 2005; Vogel and Stedinger, 1987) is an automated equivalent of the Rippl Mass Diagram Approach, one of the first methods to calculate a reservoir’s storage requirement. The design storage of Oologah Lake has been determined with this method as well. We chose this method, because it is able to combine consecutive smaller drought events into one large drought event.

With SPA, the required storage $K_t$ is calculated over a period of record of streamflow $Q_t$, given a required release $R_t$ (Eq. 1). The design storage equals the maximum value of $K_t$, see Fig. 2.

$$K_t = \begin{cases} R_t - Q_t + K_{t-1} & \text{if positive} \\ 0 & \text{otherwise} \end{cases}$$  (1)

The onset ($t_{on}$) of an event is where $K_t$ becomes positive, and the offset ($t_{off}$) is where $K_t$ reaches its maximum value (Hisdal and Tallaksen, 2000). The event duration is thus defined as:

$$\text{duration} = t_{off} - t_{on}$$  (2)
We can now calculate the drought volume:

\[
\text{volume} = \sum_{t_{\text{on}}}^{t_{\text{off}}} (R_t - Q_t) = K_{t_{\text{off}}}
\] (3)

The SPA method was applied on each of the available inflow time series. For each of the time series, the following steps were taken:

- Selection of periods during which \( K_t > 0 \);
- Store start date of each period: the onset of the drought event;
- Find the date where \( K_t \) reaches its maximum value: the offset of the drought event;
- Go back to original streamflow series and select the part from onset to offset; this is the input time series for the water balance model.

Each of the 150 year streamflow timeseries yielded several drought events with different characteristics (duration and volume).

### 2.3 Water supply loss function

For municipal water use, the economic impact of drought can be expressed in terms of change in welfare. One of many ways to estimate change in welfare is through willingness-to-pay (WTP) (Dixon et al., 1996). WTP in a drought context is the sum that individuals and businesses are willing to pay to avoid the drought. WTP can be estimated as a function of the amount of available water, the baseline water use (water use when there are no shortages), water rate and price elasticity, see Eq. (4) (Dixon et al., 1996).

\[
\text{WTP}(Q) = P_0 \left( 1 - \frac{1}{\eta} \right)(Q_0 - Q) + \frac{P_0}{2\eta Q_0}(Q_0^2 - Q^2)
\] (4)
where: \( WTP = \) willingness-to-pay [USD]; \( P_0 = \) water rate [USD m\(^{-3}\)]; \( Q_0 = \) baseline water use [m\(^3\)]; \( Q = \) water available from reservoir [m\(^3\)]; \( \eta = \) price elasticity [–].

As suggested by Brozović et al. (2007), we can assume that in case of 100% water shortage, a government would supply the basic water needs for drinking and sanitation by trucking in water from a different source (e.g. a different reservoir). An estimate for trucking cost was taken from the guidebook of the US National Cooperative Highway Research Program in 1995 (NCHRP, 1995). They give an estimate of USD 0.0885 t\(^{-1}\) mile\(^{-1}\) in the year 1995, including 45% empty miles. For the year 2013 this equals USD 0.1309 t\(^{-1}\) mile\(^{-1}\) (based on consumer price indices of 152.4 in 1995 and 233.4 in 2013) and USD 0.086 m\(^{-3}\) km\(^{-1}\) (0.95 m\(^3\) water weights about 1 t).

The monthly costs \( (C) \) involved with trucking in water are thus:

\[
C(Q_T) = C_T \cdot x \cdot Q_T
\]  

(5)

where: \( C_T = \) water trucking price [USD m\(^{-3}\) km\(^{-1}\)]; \( x = \) trucking distance [km]; \( Q_T = \) water volume to be trucked [m\(^3\)].

The basic water requirement BWR (m\(^3\) month\(^{-1}\)) can be calculated by assuming that 10% of the baseline municipal water use \( (Q_0) \) is needed for drinking and sanitation. If the water supply \( Q \) from the reservoir is less than BWR, we assume that the government will truck in a water volume of \( (BWR - Q) \). These are the additional cost on top of WTP(BWR). The total losses associated with water supply deficit \( (L_{WS}) \) are calculated by combining Eqs. (5) and (6):

\[
L_{WS} = \begin{cases} 
WTP(Q) & \text{for } BWR \leq Q < Q_0 \\
C(BWR - Q) + WTP(BWR) & \text{for } Q < BWR 
\end{cases}
\]  

(6)

When reservoir outflow \( Q \) is smaller than BWR, the government has a cost of providing enough water to obtain BWR, and individuals have a cost of having less water than their baseline use. In practice, however, it may be technically difficult for a water authority to pump very small amounts of water through their distribution network. The resulting loss
function is given in Fig. 3, which shows the loss $L_{WS}$ as a function of reservoir outflow $Q$.

We used the following values for the case:

- The consumer price for municipal water $P_0 = USD 0.84 m^{-3}$ (USD 0.00318 gallon$^{-1}$) (Tulsa, 2013);
- Average municipal water demand $Q_0 = 17.4 m^3 s^{-1}$ (Ref) and $Q_0 = 15 m^3 s^{-1}$ (S1);
- Price elasticity $\eta = -0.41$ (Dalhuisen et al., 2003);
- Trucking distance $x = 290 km$, assuming that water will be trucked in from the Kaw reservoir 145 km (90 miles) away, which is 290 km roundtrip.

2.4 Scoring the robustness criteria

To draw the response curve of the drought risk system, the disturbance was quantified by the drought volume: the cumulative difference between inflow and demand over the duration of the drought event. The drought impact (response) was quantified as the total loss in USD as a result of this drought event. The response curve was then used to score the robustness criteria.

The resistance threshold was quantified as the largest drought volume that first causes drought impact. When this is divided by the largest drought volume considered, a value between 0 and 1 is obtained.

The proportionality was scored by visually detecting sudden changes in drought impact with increasing drought volume. Proportionality is scored high when no sudden changes are detected, and low when the impact increases from zero to maximum impact as a result of a small increase in drought volume.

The manageability was scored by looking at the steepness of the curves. If the curve is less steep than the reference, impacts are smaller and larger drought volumes are needed to cause the same level of impact.
3 Results

Figure 4 shows the response curves of all configurations. Each curve is a combination of points representing a single drought event. The figure also shows linear fits through all data points of one configuration. The curves clearly differ between the configurations.

The resistance threshold in the reference is similar to the reservoir capacity. This was to be expected, since the reference assumed no hedging so that drought impacts only occur when the drought volume exceeds the reservoir capacity. This means that the system can withstand drought events until a drought volume of \(5.4 \times 10^8\) m\(^3\). The maximum volume of all considered drought events is about \(14 \times 10^8\), thus the system can withstand about 40\% of the total drought range considered. The resistance threshold therefore scores 0.4 on a scale of 0 to 1. The water supply reliability of the reference is estimated between 0.96 and 1, depending on the climate change scenario. The supply reliability was calculated for each of the 112 streamflow series (based on projections of future climate). Some of these series did not contain any drought event with a volume exceeding the reservoir capacity. This explains the supply reliability of 1. This points at a likely wetter climate according some of the climate scenarios, but it does not mean that drought events will never occur in these futures. Because the length of each streamflow series was limited (150 years), it may be a coincidence that extreme drought events with a small occurrence probability did not occur.

The resistance threshold is increased to 0.5 (\(\sim 7 \times 10^8\) m\(^3\)), by either reducing demand (S1) or by increasing supply (S3). The supply reliability is increased in both alternatives to 0.98–1. The hedging option (S2) decreases the resistance threshold to 0.35 and the supply reliability to 0.94–1. Because the outflow is temporarily reduced already when there is still water available from the reservoir, impacts start to occur at smaller drought volumes.

The S1 curve is the least steep one of all the curves, pointing to the fact that a smaller demand (the amount people are used to) also cost less to replace when this amount is
lacking. Demand reduction thus increases the drought manageability, because it takes larger droughts before a societally unacceptable level of drought impact is reached. The S3 curve is as steep as the reference, so manageability is comparable. However, because of the higher resistance threshold the total impact remains smaller than that of the reference configuration. S3 thus increases the robustness to drought events.

The S2 curve is less steep than the reference curve for small droughts and as steep for more extreme droughts. Thus, the impact is larger than in the reference between about 4 and 7 $\times$ $10^8$ m$^3$ drought volume. This is because the outflow is reduced before the reservoir is empty. At a volume of about 7 $\times$ $10^8$ m$^3$ the reservoir is empty and impact increases with the same rate as in the reference. However, impacts remain smaller than in the reference for large drought volumes. Thus, hedging is beneficial in terms of reducing impact due to extreme droughts, but the impact is increased for the more frequent droughts. In sum, the manageability is equal to the reference.

4 Discussion, conclusions and recommendations

4.1 Discussion and conclusions

The aim of this paper was to develop system robustness analysis for drought risk management. To that end, the existing framework for robustness analysis, originally developed for floods, was adapted for droughts and illustrated with a drought case. The results showed that different types of measures (demand reduction, supply increase and hedging) score differently on two of the three robustness criteria: resistance threshold and manageability. The third criterion, proportionality, did not distinguish between the system configurations. This could however change when different types of measures are considered.

The case clearly showed the different effect of increasing water supply and reducing water demand. If demand is smaller, impacts will start at larger droughts and impacts are lower over the entire range of drought magnitudes. Demand reduction thus scores
higher on both resistance threshold and manageability, and is therefore advocated from a robustness perspective. If only the supply reliability (the traditional decision criterion) were used, both measures would have been perceived comparable. This means that the decision between these two measures would mainly depend on the cost involved (besides side-effects on sustainability criteria such as environmental impact). The robustness criteria show the additional benefit of demand reduction which may be worth the investment.

Implementing hedging rules reduced the resistance threshold: impacts will start at smaller droughts. However, these impacts do not increase as fast as in the reference and total impact from extreme drought events is lower than that of the reference. The system configuration with hedging rules thus scores higher on manageability. However, the question is whether the lower score on one robustness criterion outweighs the higher score on the other robustness criterion. Furthermore, the effect of hedging highly depends on the type of loss function and the demand reduction factor, and could thus be different for other system configurations and other systems.

Although the resistance threshold is scored on a scale between 0 and 1, this does not mean that a score of 1 should be the ultimate goal. The resistance threshold is intended to inform about which range of drought events the system can withstand (zero impact), in this case 40% of the total range considered. The score is expected to raise awareness about the possibility of larger events (the other 60% of the total range considered: the “extreme range”) that the system cannot withstand; thus for which impacts are expected. The second criterion, manageability, then informs about how well the system can cope with the impacts of drought events in the extreme range.

The total range of drought events considered is a subjective choice. In this case it was chosen to select drought events from a long time series of projected streamflow, according to several climate change scenarios. This shows how severe drought events may become, without having to judge about the likelihood of the climate scenarios. How the future will develop is uncertain, but because drought events originate from climate variability (also in the current climate), the possibility of extreme drought events...
is certain. Thus, it is certain that extreme drought events will occur at some point, but it is uncertain when. Against this background it may be wise to consider a higher level of manageability, since resistance cannot eliminate the certainty of a drought event. Decision makers still have to decide on the range of drought events for which to prepare management plans and the required level of manageability. A system that is robust for the chosen range of events will most likely be robust for even more extreme events as well.

The illustrative case has demonstrated that a robustness analysis provides additional insight into how a system responds to droughts, compared to the traditional decision criterion *water supply reliability*. Because the impact of drought is expressed in economic terms, and a wide range of drought events is considered, the robustness approach fits well with the move towards risk-based drought management. Furthermore, the analysis does not depend on assumptions about how the future climate develops; instead it takes into account a wide range of possible drought events resulting from climate variability. We thus consider robustness analysis promising as part of drought risk management under climate change uncertainty.

### 4.2 Recommendations

Compared to the applications of the robustness framework on floods (Mens and Klijn, 2014; Mens et al., 2014), the impacts in this case were not compared with a recovery threshold. Exceeding a recovery threshold means that impacts are unacceptable in the sense that recovery will be very difficult, costly and time-consuming. It is recommended that future drought applications compare the impacts with a recovery threshold.

For future applications it is recommended to take into account the impact on various water users, instead of only municipal water use. This makes a robustness analysis more interesting, because it allows testing different short-term drought management strategies, for example those that prioritize water supply among users during a drought.
Acknowledgements. Thanks are due to the US Army Corps of Engineers (Institute for Water Resources and Tulsa District) for their support in carrying out the research reported in this paper. The work was partially funded by the Netherlands Knowledge for Climate program.

References


Figure 1. Example response curve: relationship between drought severity and drought impact, and robustness criteria.
Figure 2. Example of sequent peak algorithm: (upper panel) time series of streamflow ($Q_t$) and required release ($R_t$), and (lower panel) corresponding storage requirement: the reservoir would be designed based on the maximum value.
Figure 3. Loss for municipal water users as a function of reservoir outflow (for 1 month), based on reference water demand.
Figure 4. Response curves of the reference configuration (REF) and of the alternative configurations with implemented strategies (S1, S2 and S3)